

**ECONOMIC GROWTH**

**PER CAPITA INCOME OF SELECTED COUNTRIES, 2004 (IN US \$)**

Norway	43,350	Saudi Arabia	8,530
Switzerland	39,880	Mexico	6,230
United States	37,610	Malaysia	3,780
Japan	34,510	Brazil	2,710
United Kingdom	28,350	Russia	2,610
Belgium	25,820	Egypt	1,390
Germany	25,250	China	1,100
France	24,770	Indonesia	810
Australia	21,650	India	530
Italy	21,560	Pakistan	470
Kuwait	16,340	Bangladesh	400
Korea	12,020	Nigeria	320

**THE SOLOW GROWTH MODEL**

Robert Solow won Nobel Prize for contributions to the study of economic growth. It is a major paradigm which is widely used in policy making and a benchmark against which most recent growth theories are compared. The Solow Growth Model is designed to show how growth in the capital stock, growth in the labor force, and advances in technology interact in an economy, and how they affect a nation's total output of goods and services.

**HOW SOLOW MODEL IS DIFFERENT: ASSUMPTIONS**

**K** Capital (K) and Labor (L) are no longer fixed: In this model, investment leads to the growth of the capital stock (K), while depreciation causes it to shrink over time. Similarly, the labor force (L) grows due to population growth. (We can still do fiscal policy experiments)

• Cosmetic differences.

**THE PRODUCTION FUNCTION**

Let's analyze the supply and demand for goods, and see how much output is produced at any given time and how this output is allocated among alternative uses. The production function represents the transformation of inputs (labor (L), capital (K), and production technology) into outputs (final goods and services for a certain time period).

In aggregate terms:  $Y = F(K, L)$

$y = Y/L$  = output per worker

$k = K/L$  = capital per worker

Assume constant returns to scale:

$zY = F(zK, zL)$  for any  $z > 0$

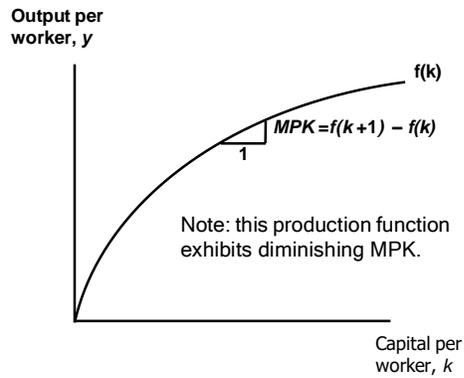
Pick  $z = 1/L$ . Then

$Y/L = F(K/L, 1)$

$y = F(k, 1)$

$y = f(k)$

Where  $f(k) = F(k, 1)$



**THE NATIONAL INCOME IDENTITY**

$Y = C + I$  (remember, no G)

In “per worker” terms:  $y = c + i$

where  $c = C/L$  and  $i = I/L$

**THE CONSUMPTION FUNCTION**

$s$  = the saving rate, the fraction of income that is saved ( $s$  is an exogenous parameter).

**Note:**  $s$  is the only lowercase variable that is not equal to its uppercase version divided by  $L$ .

Consumption function:  $c = (1-s) y$  (per worker)

**SAVING AND INVESTMENT**

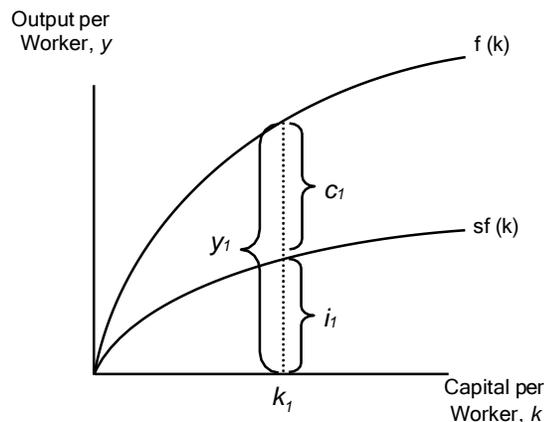
Saving (per worker) =  $sy$

National income identity is  $y = c + i$

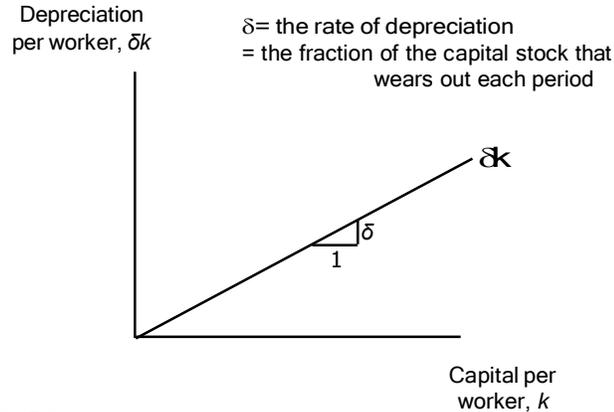
Rearrange to get:  $i = y - c = sy$  (investment = saving)

Using the results above,  $i = sy = sf(k)$

**OUTPUT, CONSUMPTION, AND INVESTMENT**



**DEPRECIATION**



**CAPITAL ACCUMULATION**

Investment makes the capital stock bigger, depreciation makes it smaller.  
 Change in capital stock = investment – depreciation

$$\Delta k = i - \delta k$$

Since  $i = sf(k)$ , this becomes:  $\Delta k = sf(k) - \delta k$

**THE EQUATION OF MOTION FOR  $k$**

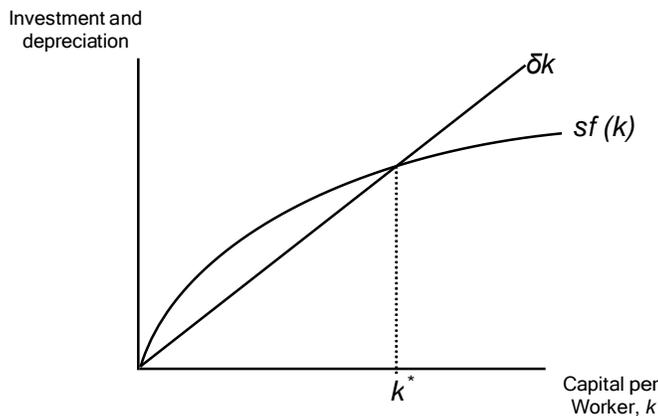
The equation of motion for  $k$  can be written as:

$$\Delta k = sf(k) - \delta k$$

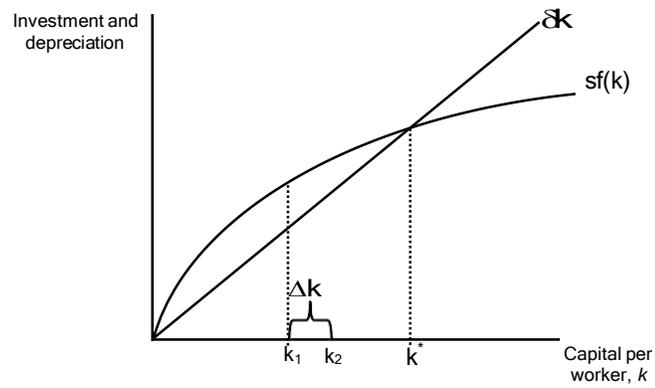
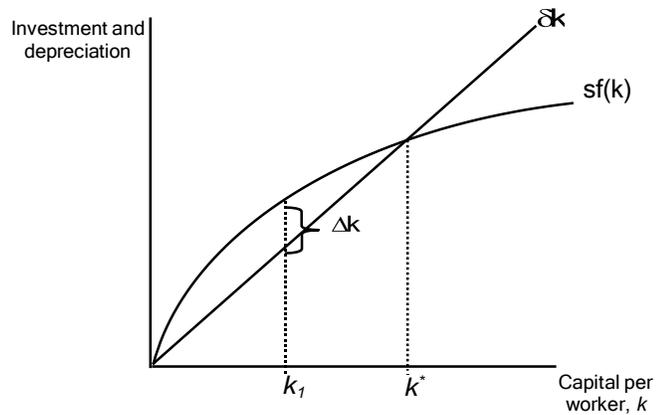
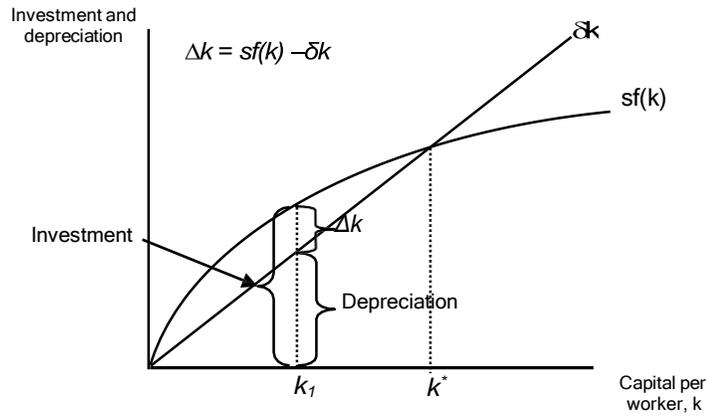
It is the Solow model's central equation. It determines behavior of capital over time which, in turn, determines behavior of all of the other endogenous variables because they all depend on  $k$ . e.g. Income per person:  $y = f(k)$ , Consumption per person:  $c = (1-s)f(k)$

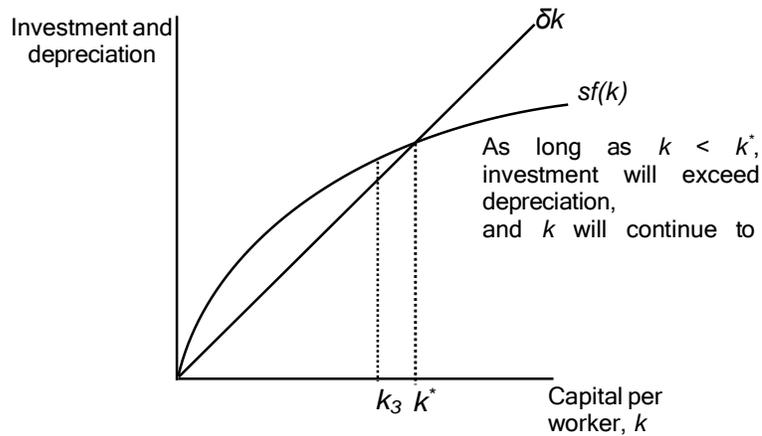
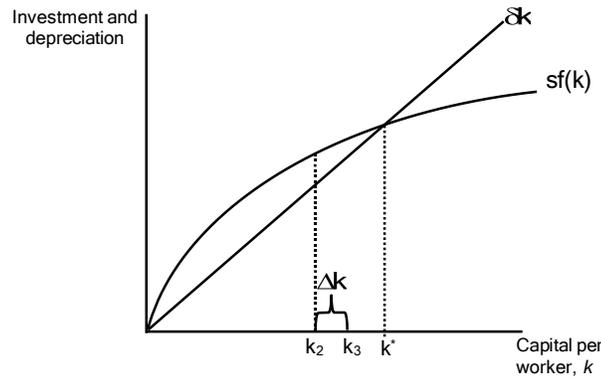
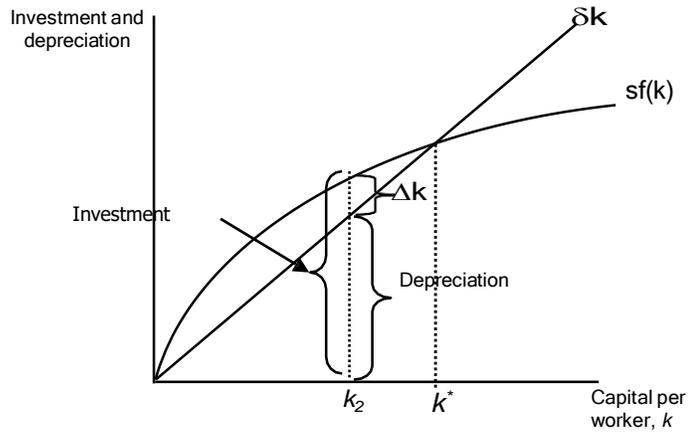
**THE STEADY STATE**

If investment is just enough to cover depreciation, [ $sf(k) = \delta k$ ], then capital per worker will remain constant:  $\Delta k = 0$ . This constant value, denoted  $k^*$ , is called the steady state capital stock.



**ECONOMIC GROWTH (CONTINUED)**  
**MOVING TOWARDS THE STEADY STATE**

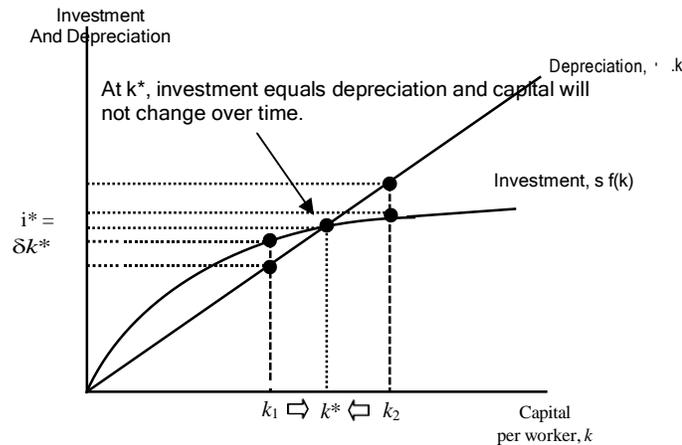




**Exercise Questions:**

- Draw the Solow model diagram, labeling the steady state  $k^*$ .
- On the horizontal axis, pick a value greater than  $k^*$  for the economy's initial capital stock. Label it  $k_1$ .
- Show what happens to  $k$  over time.
- Does  $k$  move toward the steady state or away from it?

**THE STEADY STATE**



**A NUMERICAL EXAMPLE**

Production function (aggregate):

$$Y = F(K, L) = \sqrt{K \times L} = K^{1/2} L^{1/2}$$

To derive the per-worker production function, divide through by  $L$ :

$$\frac{Y}{L} = \frac{K^{1/2} L^{1/2}}{L} = \left(\frac{K}{L}\right)^{1/2}$$

Then substitute  $y = Y/L$  and  $k = K/L$  to get

$$y = f(k) = k^{1/2}$$

Assume:  $s = 0.3$ ,  $\delta = 0.1$ , initial value of  $k = 4.0$

**APPROACHING THE STEADY STATE**

Year	$k$	$y$	$c$	$i$	$\delta k$	$\Delta k$
1	4.000	2.000	1.400	0.600	0.400	0.200
2	4.200	2.049	1.435	0.615	0.420	0.195
3	4.395	2.096	1.467	0.629	0.440	0.189
4	4.584	2.141	1.499	0.642	0.458	0.184
			...			
10	5.602	2.367	1.657	0.710	0.560	0.150
			...			
25	7.351	2.706	1.894	0.812	0.732	0.080
			...			
100	8.962	2.994	2.096	0.898	0.896	0.002
			...			
$\infty$	9.000	3.000	2.100	0.900	0.900	0.000

**EXERCISE: SOLVE FOR THE STEADY STATE**

Continue to assume  $s = 0.3$ ,  $\delta = 0.1$ , and  $y = k^{1/2}$

Use the equation of motion:  $\Delta k = s f(k) - \delta k$  to solve for the steady-state values of  $k$ ,  $y$ , and  $c$ .

**Solution:**

$\Delta k = 0$  def. of steady state

$s f(k^*) = \delta k^*$  eq'n of motion with  $\Delta k = 0$

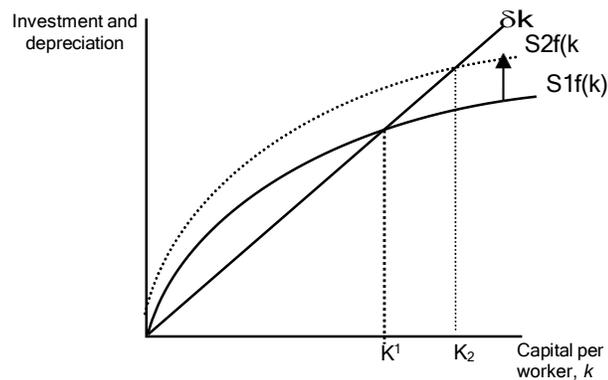
$0.3\sqrt{k^*} = 0.1k^*$  using assumed values

$$3 = \frac{k^*}{\sqrt{k^*}} = \sqrt{k^*}$$

Solve to get:  $k^* = 9$  and  $y^* = \sqrt{k^*} = 3$

Finally,  $c^* = (1-s)y^* = 0.7 \times 3 = 2.1$

### AN INCREASE IN THE SAVING RATE



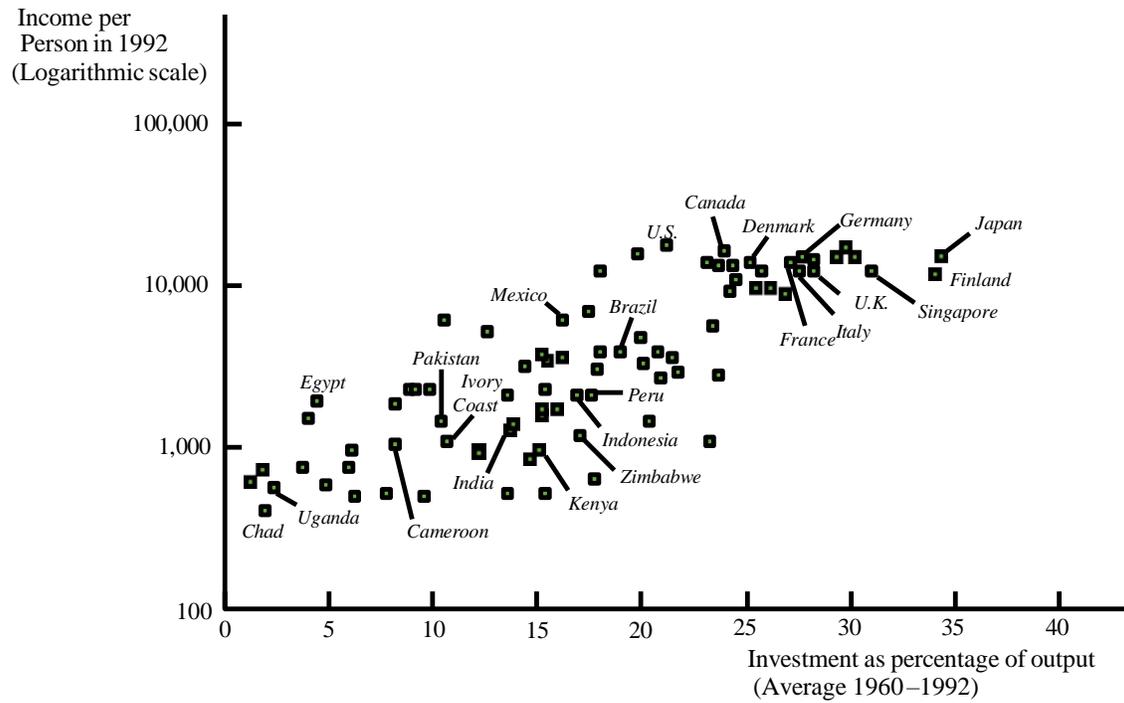
An increase in the saving rate raises investment causing the capital stock to grow toward a new steady state

#### PREDICTION:

Higher  $s \Rightarrow$  higher  $k^*$ , and since  $y = f(k)$ , higher  $k^* \Rightarrow$  higher  $y^*$ .

Thus, the Solow model predicts that countries with higher rates of saving and investment will have higher levels of capital and income per worker in the long run.

**INTERNATIONAL EVIDENCE ON INVESTMENT RATES AND INCOME PER PERSON**



ECONOMIC GROWTH (CONTINUED)

THE GOLDEN RULE

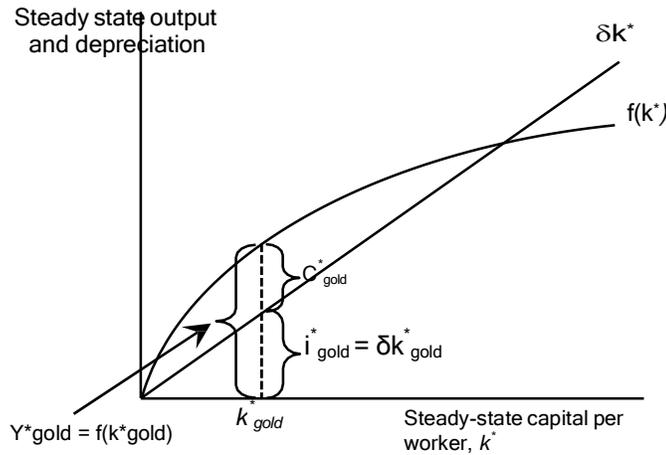
Different values of  $s$  lead to different steady states. How do we know which is the “best” steady state? Economic well-being depends on consumption, so the “best” steady state has the highest possible value of consumption per person:  $c^* = (1-s) f(k^*)$ . An increase in  $s$  leads to higher  $k^*$  and  $y^*$ , which may raise  $c^*$  and reduces consumption’s share of income  $(1-s)$ , which may lower  $c^*$ . So, how do we find the  $s$  and  $k^*$  that maximize  $c^*$ ?

THE GOLDEN RULE LEVEL OF CAPITAL STOCK

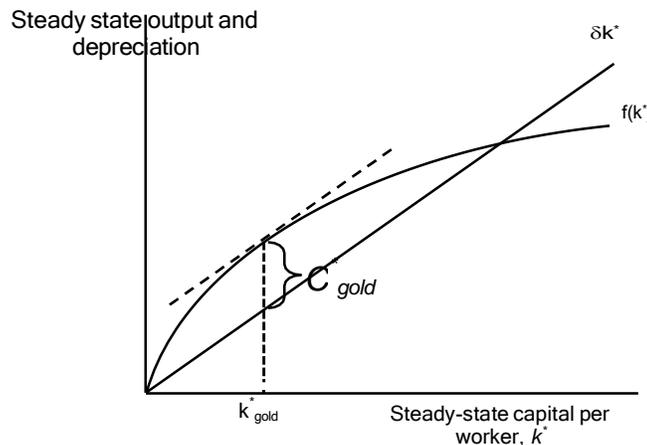
$K^*_{gold}$  = the Golden Rule level of capital, the steady state value of  $k$  that maximizes consumption. To find it, first express  $c^*$  in terms of  $k^*$ :

$$\begin{aligned} c^* &= y^* - i^* \\ &= f(k^*) - i^* \\ &= f(k^*) - \delta k^* \end{aligned}$$

In general:  $i = \Delta k + \delta k$ , in the steady state:  $i^* = \delta k^*$  because  $\Delta k = 0$ . Then, graph  $f(k^*)$  and  $\delta k^*$ , and look for the point where the gap between them is biggest.



$c^* = f(k^*) - \delta k^*$  is biggest where the slope of the production function equals the slope of the depreciation line:  $MPK = \delta$ .



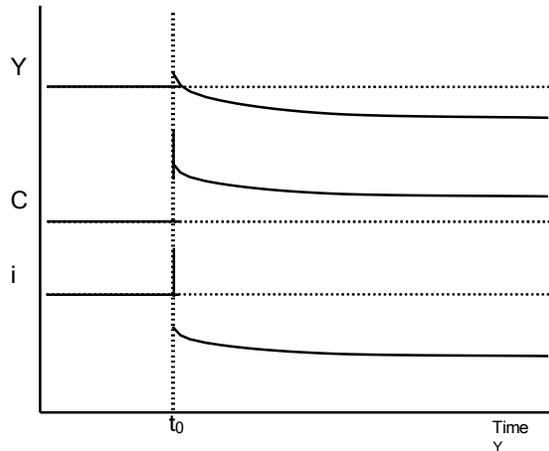
**THE TRANSITION TO THE GOLDEN RULE STEADY STATE**

The economy does NOT have a tendency to move toward the Golden Rule steady state. Achieving the Golden Rule requires that Policymakers adjust  $s$ . This adjustment leads to a new steady state with higher consumption. But what happens to consumption during the transition to the Golden Rule?

**STARTING WITH TOO MUCH CAPITAL**

If  $k^* > k_{gold}^*$

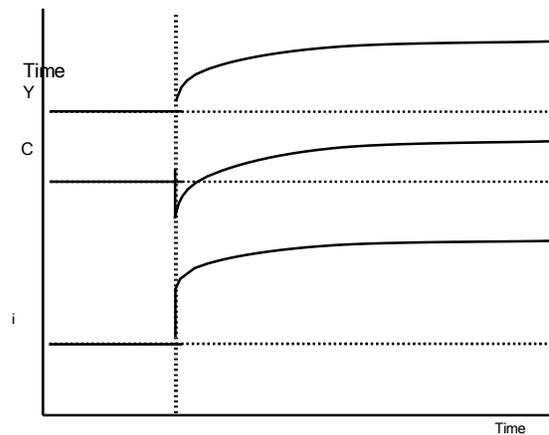
Then increasing  $c^*$  requires a fall in  $s$ . In the transition to the Golden Rule, consumption is higher at all points in time.



**STARTING WITH TOO LITTLE CAPITAL**

If  $k^* < k_{gold}^*$

Then increasing  $c^*$  requires an increase in  $s$ . Future generations enjoy higher consumption, but the current one experiences an initial drop in consumption.



The basic Solow model cannot explain sustained economic growth. It simply says that high rates of saving lead to high growth temporarily, but the economy eventually approaches a steady state. We need to incorporate two sources of growth to explain sustained economic growth: population and technological progress.

**POPULATION GROWTH**

Assume that the population--and labor force-- grow at rate  $n$ . ( $n$  is exogenous)

$$\frac{\Delta L}{L} = n$$

Suppose  $L = 1000$  in year 1 and the population is growing at 2%/year ( $n = 0.02$ ). Then  $\Delta L = n L = 0.02 \times 1000 = 20$ , so  $L = 1020$  in year 2.

**BREAK-EVEN INVESTMENT**

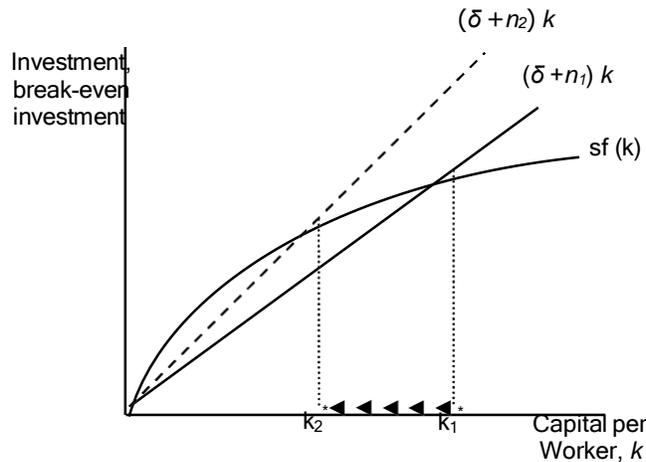
$(\delta + n) k$  = break-even investment, the amount of investment necessary to keep  $k$  constant.

- Break-even investment includes:
- $\delta k$  to replace capital as it wears out.
- $nk$  to equip new workers with capital. (Otherwise,  $k$  would fall as the existing capital stock would be spread more thinly over a larger population of workers).

**THE EQUATION OF MOTION FOR  $k$**

With population growth, the equation of motion for  $k$  is  $\Delta k = s f(k) - (\delta + n) k$ . Where  $S f(k)$  = actual investment,  $(\delta + n) k$  = breakeven investment.

**THE IMPACT OF POPULATION GROWTH**



**PREDICTION:**

Higher  $n \Rightarrow$  lower  $k^*$ , and since  $y = f(k)$ , lower  $k^* \Rightarrow$  lower  $y^*$ .

Thus, the Solow model predicts that countries with higher population growth rates will have lower levels of capital and income per worker in the long run.

**THE GOLDEN RULE WITH POPULATION GROWTH**

To find the Golden Rule capital stock, we again express  $c^*$  in terms of  $k^*$ :

$$\begin{aligned} c^* &= y^* - i^* \\ &= f(k^*) - (\delta + n)k^* \end{aligned}$$

$c^*$  is maximized when

$$MPK = \delta + n$$

Or equivalently,

$$MPK - \delta = n$$

In the Golden Rule Steady State, the marginal product of capital net of depreciation equals the population growth rate.

**ECONOMIC GROWTH (CONTINUED)**

Previously, in the Solow model,

- The production technology was held constant
- Income per capita was constant in the steady state.

Neither point is true in the real world

**TECHNOLOGICAL PROGRESS IN THE SOLOW MODEL**

A new variable:  $E$  = labor efficiency. Assume: Technological progress is labor-augmenting: it increases labor efficiency at the exogenous rate  $g$ :

$$g = \frac{\Delta E}{E}$$

We now write the production function as:

$$Y = F ( K , L \times E )$$

Where  $L \times E$  = the number of effective workers. Hence, increases in labor efficiency have the same effect on output as increases in the labor force.

**Notations:**  $y = Y/LE$  = output per effective worker  
 $k = K/LE$  = capital per effective worker

Production function per effective worker:  $y = f(k)$

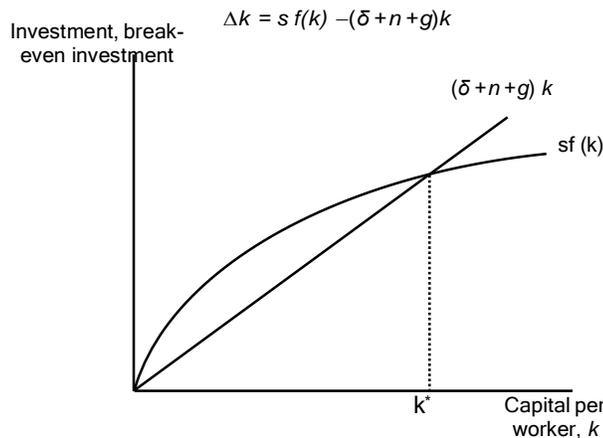
Saving and investment per effective worker:  $s y = s f(k)$

$(\delta + n + g) k$  = break-even investment: the amount of investment necessary to keep  $k$  constant. This consists of:

$\delta k$  to replace depreciating capital

$n k$  to provide capital for new workers

$g k$  to provide capital for the new “effective” workers created by technological progress



**STEADY-STATE GROWTH RATES IN THE SOLOW MODEL WITH TECHNOLOGICAL PROGRESS**

Variable	Symbol	Steady-State growth rate
Capital per effective worker	$k = K/(L \times E)$	0
Output per effective worker	$y = Y/(L \times E)$	0
Output per worker	$(Y/L) = y \times E$	$G$
Total output	$Y = y \times E \times L$	$n + g$

**THE GOLDEN RULE WITH TECHNOLOGICAL PROGRESS**

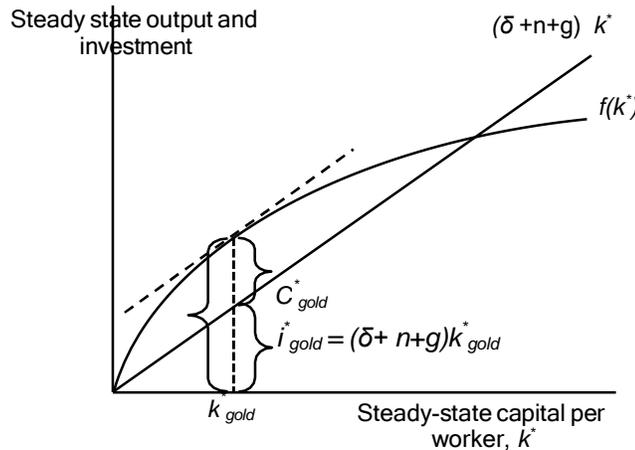
To find the Golden rule capital stock, express  $c^*$  in terms of  $k^*$ :

$$c^* = y^* - i^* = f(k^*) - (\delta + n + g) k^*$$

$c^*$  is maximized when  $MPK = \delta + n + g$

Or equivalently,  $MPK - \delta = n + g$

In the Golden Rule Steady State, the marginal product of capital net of depreciation equals the population growth rate plus the rate of tech progress.



**POLICIES TO PROMOTE GROWTH**

Four policy questions:

- Are we saving enough? Too much?
- What policies might change the saving rate?
- How should we allocate our investment between privately owned physical capital, public infrastructure, and “human capital”?
- What policies might encourage faster technological progress?

**1. EVALUATING THE RATE OF SAVING**

Use the Golden Rule to determine whether our saving rate and capital stock are too high, too low, or about right. To do this, we need to compare  $(MPK - \delta)$  to  $(n + g)$ .

If  $(MPK - \delta) > (n + g)$ , then we are below the Golden Rule steady state and should increase  $s$ .

If  $(MPK - \delta) < (n + g)$ , then we are above the Golden Rule steady state and should reduce  $s$ .

To estimate  $(MPK - \delta)$ , we use three facts about an economy;

- $k = 2.5 y$ : the capital stock is about 2.5 times one year’s GDP.
- $\delta k = 0.1 y$ : about 10% of GDP is used to replace depreciating capital.
- $MPK \times k = 0.3 y$ : capital income is about 30% of GDP

So,

- $k = 2.5 y$
- $\delta k = 0.1 y$
- $MPK \times k = 0.3 y$

To determine  $\delta$ , divided 2 by 1:

$$\frac{\delta k}{k} = \frac{0.1 y}{2.5 y} \Rightarrow \delta = \frac{0.1}{2.5} = 0.04$$

To determine  $MPK$ , divided 3 by 1:

$$\frac{MPK \times k}{k} = \frac{0.3 y}{2.5 y} \Rightarrow MPK = \frac{0.3}{2.5} = 0.12$$

Hence,  $MPK - \delta = 0.12 - 0.04 = 0.08$

Real GDP grows an average of 3%/year, so  $n + g = 0.03$ . Thus, in this economy,  $MPK - \delta = 0.08 > 0.03 = n + g$

**Conclusion**

The economy is below the Golden Rule steady state: If we increase saving rate of this economy, the economy will have faster growth until it reaches to a new steady state with higher consumption per capita.

## ECONOMIC GROWTH (CONTINUED)

## 2. POLICIES TO INCREASE THE SAVING RATE

- Reduce the government budget deficit (or increase the budget surplus).
- Increase incentives for private saving:
- Reduce capital gains tax, corporate income tax, estate tax as they discourage saving
- Replace federal income tax with a consumption tax
- Expand tax incentives for retirement savings accounts and other retirement savings

Expand tax incentives for retirement savings accounts: By providing tax benefits for contributions to retirement accounts, individuals are encouraged to save more for their future

## 3. ALLOCATING THE ECONOMY'S INVESTMENT

In the Solow model, there's one type of capital. In the real world, there are many types, which we can divide into three categories:

- Private capital stock
- Public infrastructure
- Human capital: the knowledge and skills that workers acquire through education

How should we allocate investment among these types?

**Two viewpoints:**

1. **Equalize tax treatment** of all types of capital in all industries, and then let the market allocate investment to the type with the highest marginal product.

2. **Industrial policy:** Govt. should actively encourage investment in capital of certain types or in certain industries, because they may have positive externalities (by-products) that private investors don't consider.

**Possible problems with industrial policy**

- Does the govt. have the ability to "pick winners" (choose industries with the highest return to capital or biggest externalities)?
- Would politics rather than economics influence which industries get preferential treatment?

## 4. ENCOURAGING TECHNOLOGICAL PROGRESS

- Patent laws: encourage innovation by granting temporary monopolies to inventors of new products
- Tax incentives for R&D
- Grants to fund basic research at universities
- Industrial policy: encourage specific industries that are key for rapid tech. progress (subject to the concerns on the preceding slide)

**GROWTH EMPIRICS: CONFRONTING THE SOLOW MODEL WITH THE FACTS**

Solow model's steady state exhibits balanced growth - many variables grow at the same rate.

Solow model predicts  $Y/L$  and  $K/L$  grow at same rate ( $g$ ), so that  $K/Y$  should be constant. This is true in the real world. Solow model predicts real wage grows at same rate as  $Y/L$ , while real rental price is constant. Also true in the real world.

**CONVERGENCE**

Solow model predicts that, other things equal, "poor" countries (with lower  $Y/L$  and  $K/L$ ) should grow faster than "rich" ones. If true, then the income gap between rich & poor countries would shrink over time, and living standards "converge." In real world, many poor countries do NOT grow faster than rich ones. Does this mean the Solow model fails? No, because "other things" aren't equal. In samples of countries with similar savings & population growth rates, income gaps shrink about 2% / year. In larger samples, if one controls for differences in saving, population growth, and human capital, incomes converge by about 2%/year.

What the Solow model really predicts is conditional convergence - countries converge to their own steady states, which are determined by saving, population growth, and education. And this prediction comes true in the real world.

### FACTOR ACCUMULATION VS. PRODUCTION EFFICIENCY

Two reasons why income per capita are lower in some countries than others:

- Differences in capital (physical or human) per worker
- Differences in the efficiency of production (the height of the production function)

#### Studies:

Both factors are important.

Countries with higher capital (phys or human) per worker also tend to have higher production efficiency.

#### Explanations:

Production efficiency encourages capital accumulation.

Capital accumulation has externalities that raise efficiency.

A third, unknown variable causes cap accumulation and efficiency to be higher in some countries than others.

### ENDOGENOUS GROWTH THEORY

In Solow model, sustained growth in living standards is due to tech progress. The rate of tech progress is exogenous. While endogenous growth theory is a set of models in which the growth rate of productivity and living standards is endogenous.

#### A basic model

The production function for endogenous growth model can be written as:  $Y = A K$ , where A is the amount of output for each unit of capital (A is exogenous & constant). Key difference between this model & Solow model is that MPK is constant here while diminishes in Solow model.

Investment:  $sY$

Depreciation:  $\delta K$

Equation of motion for total capital:  $\Delta K = s Y - \delta K$

Divide through by K and use  $Y = A K$ , get:

$$\frac{\Delta Y}{Y} = \frac{\Delta K}{K} = s A - \delta$$

If  $s A > \delta$ , then income will grow forever, and investment is the “engine of growth.” Here, the permanent growth rate depends on s. In Solow model, it does not.

### DOES CAPITAL HAVE DIMINISHING RETURNS OR NOT?

Yes, if “capital” is narrowly defined (plant & equipment). Perhaps not, with a broad definition of “capital” (physical & human capital, knowledge). Some economists believe that knowledge exhibits increasing returns. In the endogenous growth model, the assumption of constant returns to capital is more plausible.

### A TWO-SECTOR MODEL

There are two sectors:

- Manufacturing firms produce goods
- Research universities produce knowledge that increases labor efficiency in manufacturing

$u$  = fraction of labor in research ( $u$  is exogenous)

- Manufacturing production function:  $Y = F [K, (1-u) E L]$
- Research production function:  $\Delta E = g(u) E$

Capital accumulation:  $\Delta K = s Y - \delta K$

In the steady state, manufacturing output per worker and the standard of living grow at rate  $\Delta E/E = g(u)$ .

Key variables are:

**s:** affects the level of income, but not its growth rate (same as in Solow model)

**u:** affects level and growth rate of income

**Question:** Would an increase in  $u$  be unambiguously good for the economy?

### THREE FACTS ABOUT R&D IN THE REAL WORLD

1. Much research is done by firms seeking profits.

2. Firms profit from research because new inventions can be patented, creating a stream of monopoly profits until the patent expires. There is an advantage to being the first firm on the market with a new product.

3. Innovation produces externalities that reduce the cost of subsequent innovation.

Much of the new endogenous growth theory attempts to incorporate these facts into models to better understand tech progress.

### IS THE PRIVATE SECTOR DOING ENOUGH R&D?

The existence of positive externalities in the creation of knowledge suggests that the private sector is not doing enough R&D. But, there is much duplication of R&D effort among competing firms. Estimates: The social return to R&D is at least 40% per year. Thus, many believe govt should encourage R&D.

## AGGREGATE DEMAND AND AGGREGATE SUPPLY

### TIME HORIZONS

- **Long run:** Prices are flexible, respond to changes in supply or demand
- **Short run:** many prices are “sticky” at some predetermined level

The economy behaves much differently when prices are sticky.

### CLASSICAL MACROECONOMIC THEORY

- Output is determined by the supply side:
- Supplies of capital, labor
- Technology
- **Changes in demand for goods & services (C, I, G) only affect prices**, not quantities.
- Complete price flexibility is a crucial assumption, so classical theory applies in the long run.

### WHEN PRICES ARE STICKY

Output and employment also depend on demand for goods & services, which is affected by: Fiscal policy ( $G$  and  $T$ ), monetary policy ( $M$ ), other factors, like exogenous changes in  $C$  or  $I$ .  
How? Why?

### THE MODEL OF AGGREGATE DEMAND AND SUPPLY

The paradigm that most mainstream economists & policymakers use to think about economic fluctuations and policies to stabilize the economy. This shows how the price level and aggregate output are determined and how the economy’s behavior is different in the short run and long run.

### AGGREGATE DEMAND

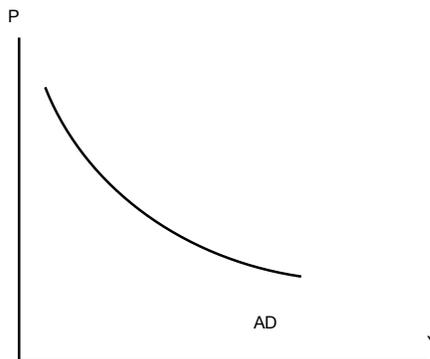
The aggregate demand curve shows the relationship between the price level and the quantity of output demanded. For an intro to the AD/AS model, we use a simple theory of aggregate demand based on the Quantity Theory of Money.

### THE QUANTITY EQUATION AS AGGREGATE DEMAND

Recall the quantity equation:  $M V = P Y$  and the money demand function it implies:  $(M/P) d = k Y$ , where  $V = 1/k =$  velocity. For given values of  $M$  and  $V$ , these equations imply an inverse relationship between  $P$  and  $Y$ .

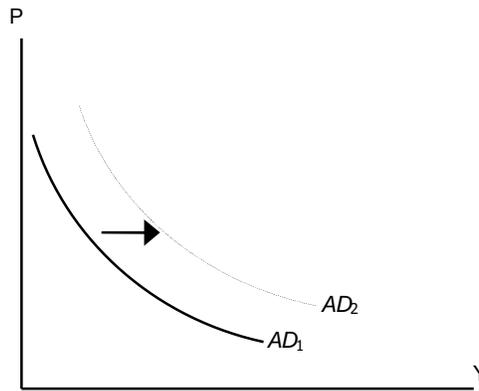
### THE DOWNWARD-SLOPING AD CURVE

An increase in the price level causes a fall in real money balances  $(M/P)$ , causing a decrease in the demand for goods & services.



**SHIFTING THE AD CURVE**

An increase in the money supply shifts the AD curve to the right.

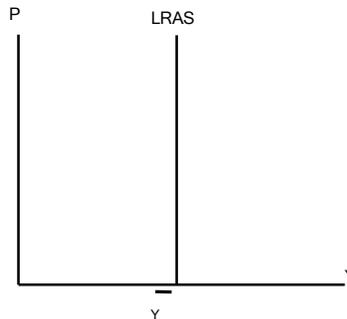


**AGGREGATE SUPPLY IN THE LONG RUN**

Recall, in the long run, output is determined by factor supplies and technology:

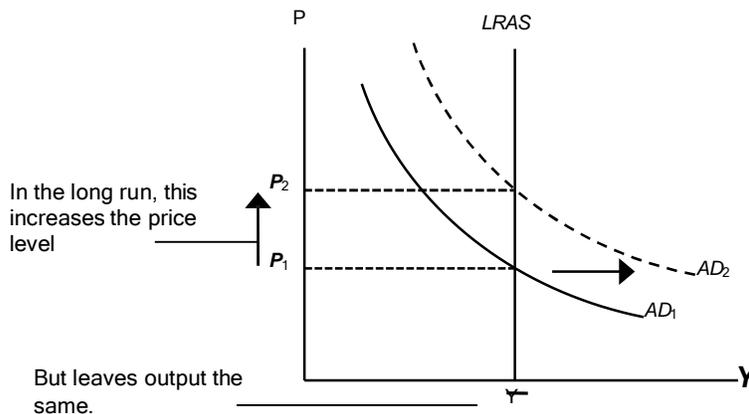
$$\bar{Y} = F(\bar{K}, \bar{L})$$

$\bar{Y}$  is the full-employment or natural level of output, the level of output at which the economy's resources are fully employed. "Full employment" means that unemployment equals its natural rate. Full-employment output does not depend on the price level, so the long run aggregate supply (LRAS) curve is vertical.



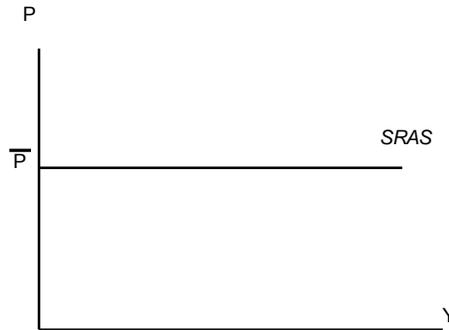
**LONG-RUN EFFECTS OF AN INCREASE IN MONEY**

An increase in M shifts the AD curve to the right.

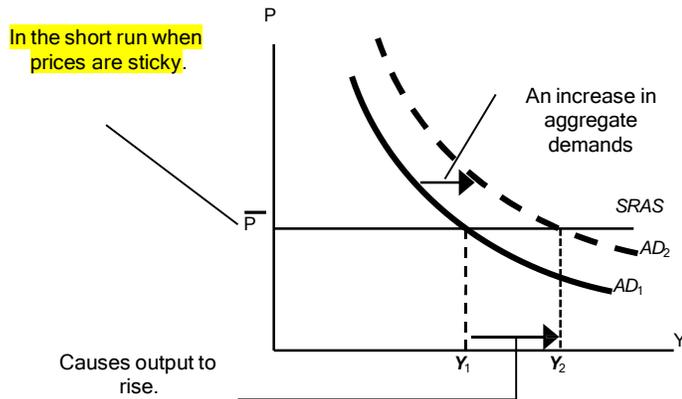


**AGGREGATE SUPPLY IN THE SHORT RUN**

In the real world, many prices are sticky in the short run. For now we assume that all prices are stuck at a predetermined level in the short run and that firms are willing to sell as much as their customers are willing to buy at that price level. Therefore, the short-run aggregate supply (SRAS) curve is horizontal. The SRAS curve is horizontal: The price level is fixed at a predetermined level, and firms sell as much as buyers demand.



**SHORT-RUN EFFECTS OF AN INCREASE IN M**

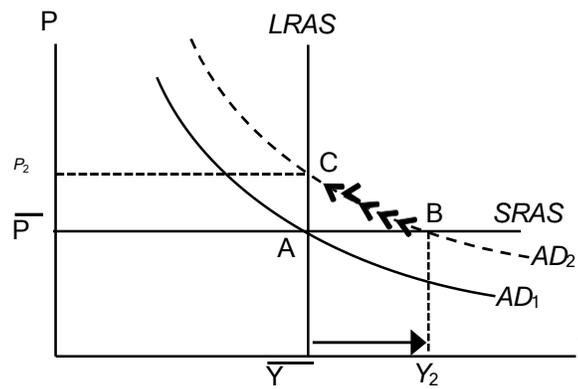


**FROM THE SHORT RUN TO THE LONG RUN**

Over time, prices gradually become “unstuck.” When they do, will they rise or fall?

In the short-run equilibrium, if	then over time, the price level will
$Y > \bar{Y}$	Rise
$Y < \bar{Y}$	Fall
$Y = \bar{Y}$	Remain constant

This adjustment of prices is what moves the economy to its long-run equilibrium.

THE SR & LR EFFECTS OF  $\Delta M > 0$ 

A = initial equilibrium

B = new short-run equilibrium after SBP increases M

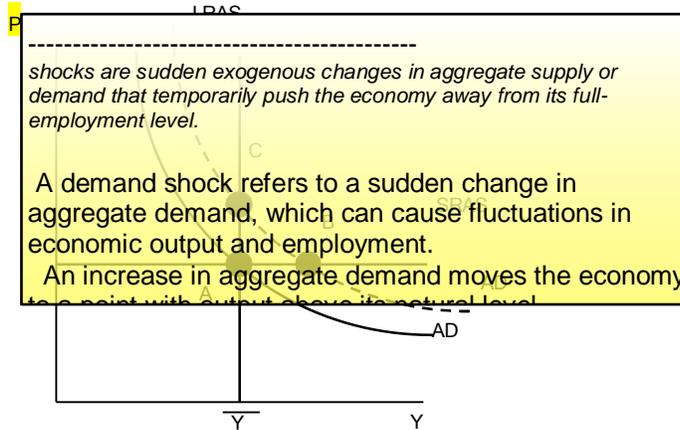
C = long-run equilibrium

**AGGREGATE DEMAND AND AGGREGATE SUPPLY (CONTINUED)**

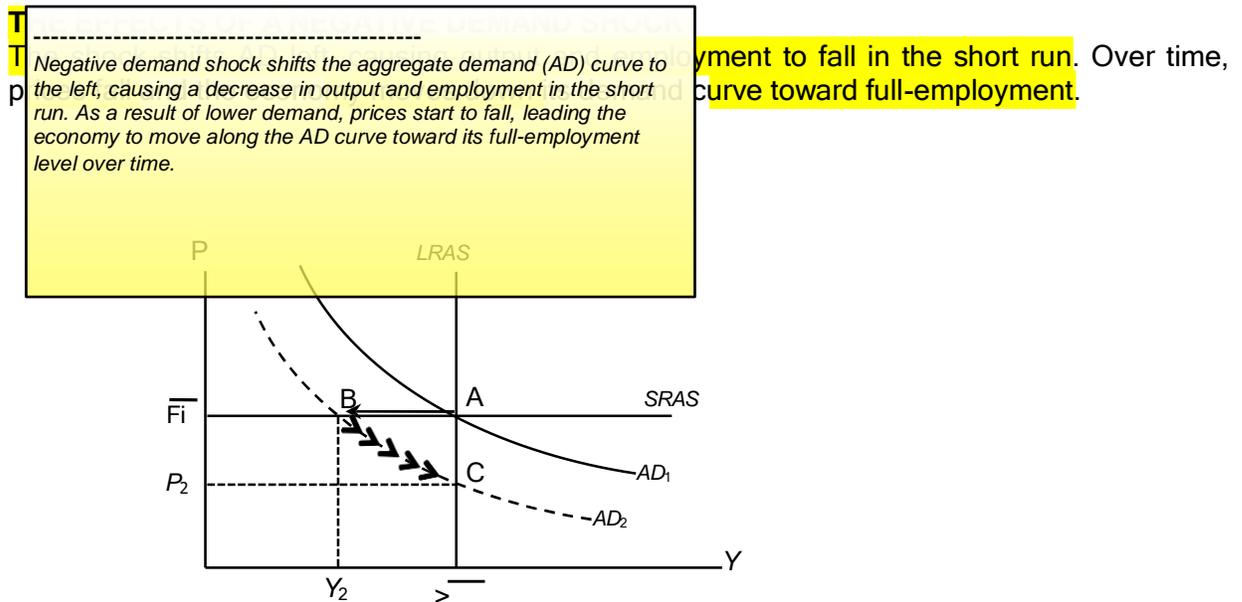
**SHOCKS:** exogenous changes in aggregate supply or demand. Shocks temporarily push the economy away from full-employment.

**A DEMAND SHOCK**

The economy begins in long-run equilibrium at point A. An increase in aggregate demand, due to an increase in the velocity of money, moves the economy from point A to point B, where output is above its natural level. As prices rise, output gradually returns to its natural rate, and the economy moves from point B to point C.



**Exogenous decrease in velocity:** If the money supply is held constant, then a decrease in  $V$  means people will be using their money in fewer transactions, causing a decrease in demand for goods and services.



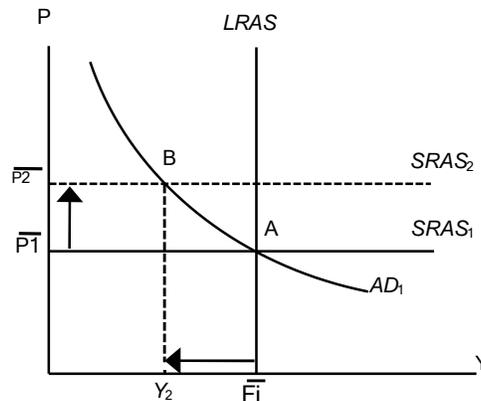
**SUPPLY SHOCKS**

A supply shock alters production costs, affects the prices that firms charge. (Also price shocks)

**Examples** of adverse supply shocks:

- Bad weather reduces crop yields, pushing up food prices.
- Workers unionize, negotiate wage increases.
- New environmental regulations require firms to reduce emissions. Firms charge higher prices to help cover the costs of compliance.

(Favorable supply shocks lower costs and prices)

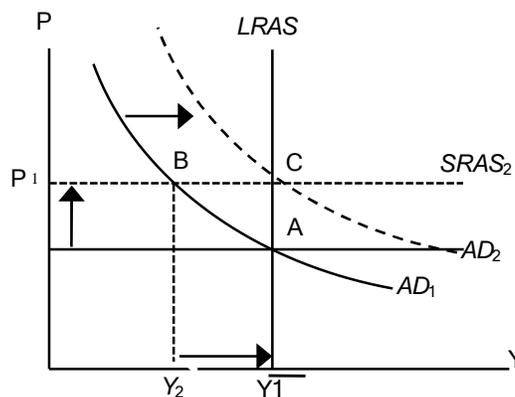


The adverse supply shock moves the economy to point B.

**STABILIZATION POLICY**

Policy actions aimed at reducing the severity of short-run economic fluctuations.

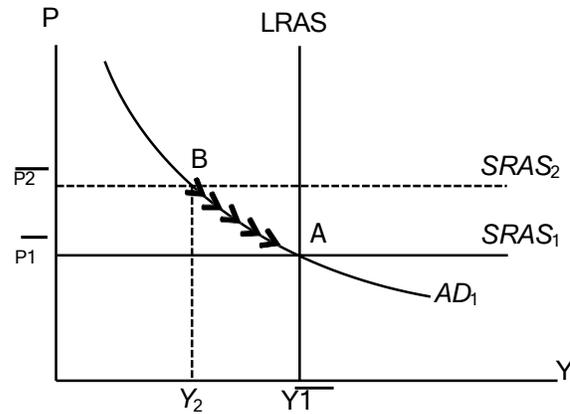
**Example:** Using monetary policy to combat the effects of adverse supply shocks. But central bank accommodates the shock by raising aggregate demand.



Results:  $P$  is permanently higher, but  $Y$  remains at its full-employment level.

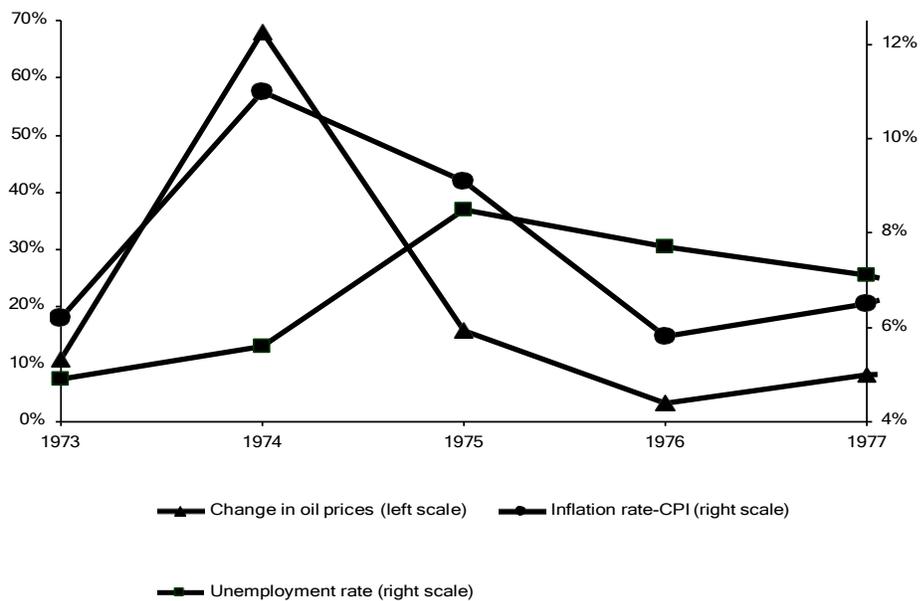
**THE 1970s OIL SHOCKS**

Early 1970s: OPEC coordinates a reduction in the supply of oil. Oil prices rose 11% in 1973, 68% in 1974, and 16% in 1975. Such sharp oil price increases are supply shocks because they significantly impact production costs and prices. The oil price shock shifts SRAS up, causing output and employment to fall. In absence of further price shocks, prices will fall over time and economy moves back toward full employment.

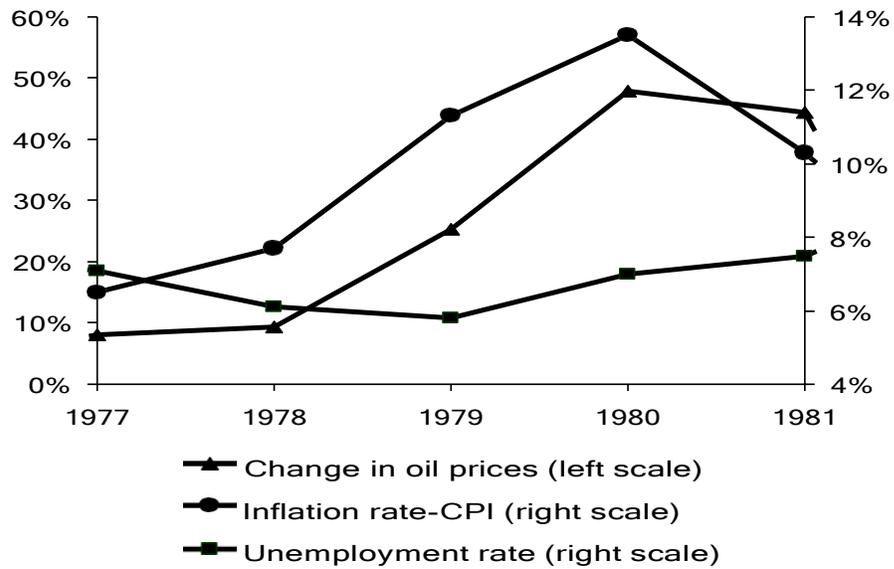


**Predicted effects of the oil price shock:**

Inflation ↑, Output ↓, Unemployment ↑ and then a gradual recovery.

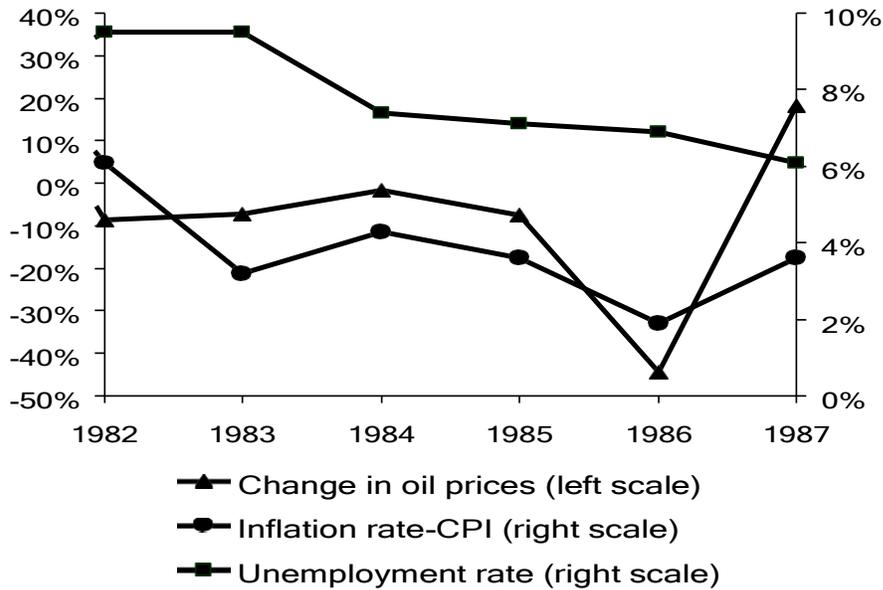


**LATE 1970s:** As economy was recovering, oil prices shot up again, causing another huge supply shock!!!



**THE 1980s OIL SHOCKS**

**1980s:** A favorable supply shock--a significant fall in oil prices. As the model would predict, inflation and unemployment fell.



**KEYNESIAN THEORY OF INCOME & EMPLOYMENT**

In long run,

- Prices flexible
- Output determined by factors of production & technology
- Unemployment equals its natural rate

In short run,

- Prices fixed
- Output determined by aggregate demand
- Unemployment is negatively related to output

**THE KEYNESIAN CROSS**

It is the simple closed economy model in which income is determined by expenditure. This model is presented by J.M. Keynes.

**Notations:**

$I$  = planned investment

$E = C + I + G$  = planned expenditure

$Y$  = real GDP = actual expenditure

**Actual expenditure** is the amount that households, firms and the government spend on goods and services; it equals the economy's gross domestic product (GDP).

**Planned expenditure** is the amount households, firms and the government would like to spend on goods and services.

**ELEMENTS OF THE KEYNESIAN CROSS**

Consumption function:

$$C = C(Y - T)$$

Govt policy variables:

$$G = \bar{G}, \quad T = \bar{T}$$

For now, investment is exogenous:

$$I = \bar{I}$$

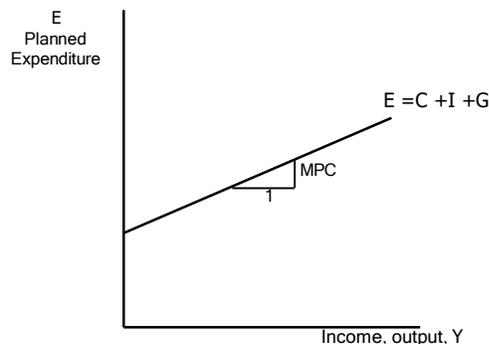
Planned expenditure:

$$E = C(Y - \bar{T}) + \bar{I} + \bar{G}$$

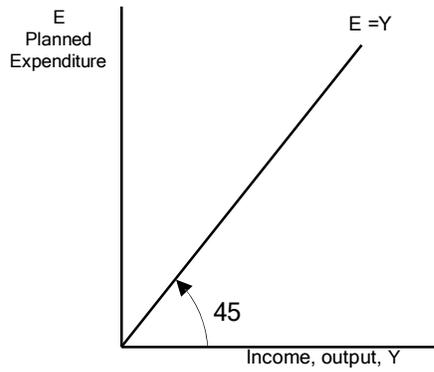
Equilibrium condition:

$$\text{Actual expenditure} = \text{Planned expenditure}$$

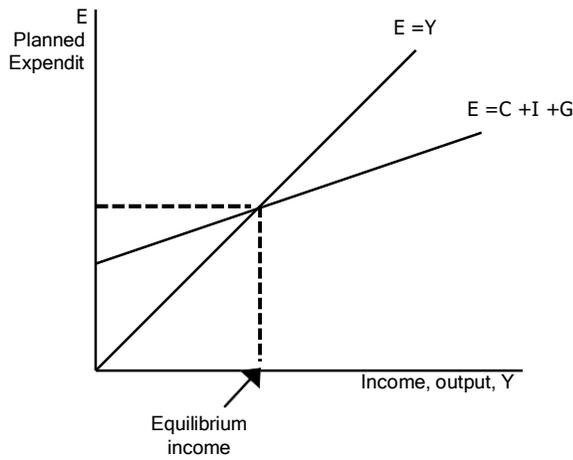
$$Y = E$$

**GRAPHING PLANNED EXPENDITURE**

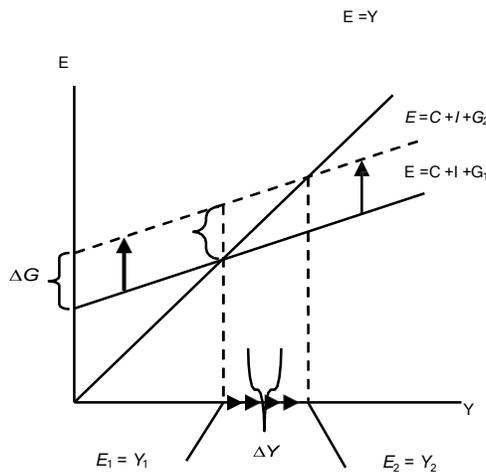
**GRAPHING THE EQUILIBRIUM CONDITION**



**THE EQUILIBRIUM VALUE OF INCOME**



**AN INCREASE IN GOVERNMENT PURCHASES**



At  $Y_1$ , there is now an unplanned drop in inventory, so firms increase output, and income rises toward a new equilibrium

**SOLVING FOR ΔY**

Equilibrium condition

$$\begin{aligned}
 Y &= C + I + G \\
 \Delta Y &= \Delta C + \Delta I + \Delta G \\
 &= \Delta C + \Delta G \\
 &= MPC \times \Delta Y + \Delta G
 \end{aligned}$$

In changes form

Since I is exogenous

Because  $\Delta C = MPC \times \Delta Y$

Collect terms with ΔY on the left side of the equals sign:  $(1 - MPC) \times \Delta Y = \Delta G$

Finally, solve for ΔY:  $\Delta Y = \left( \frac{1}{1 - MPC} \right) \times \Delta G$

**THE GOVERNMENT PURCHASES MULTIPLIER**

The increase in income resulting from Rs.1 increase in G is known as government purchases multiplier. In this model, the G multiplier equals:

$$\frac{\Delta Y}{\Delta G} = \frac{1}{1 - MPC}$$

**Example:** If MPC = 0.8

$$\begin{aligned}
 \Delta Y &= \frac{1}{1 - MPC} \Delta G \\
 &= \frac{1}{1 - 0.8} \Delta G = \frac{1}{0.2} \Delta G = 5 \Delta G
 \end{aligned}$$

The increase in G causes income to increase by 5 times as much!

In the example with MPC = 0.8,

$$\frac{\Delta Y}{\Delta G} = \frac{1}{1 - MPC}$$

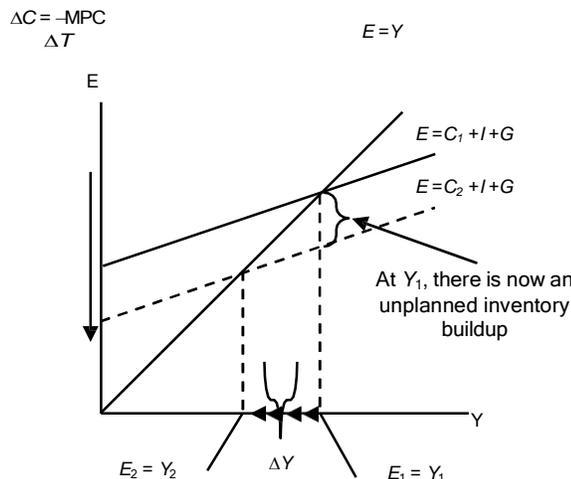
**WHY THE MULTIPLIER IS GREATER THAN 1?**

Initially, the increase in G causes an equal increase in Y:  $\Delta Y = \Delta G$ .

But  $\uparrow Y \Rightarrow \uparrow C \Rightarrow$  further  $\uparrow Y \Rightarrow$  further  $\uparrow C \Rightarrow$  Further  $\uparrow Y$

So the final impact on income is much bigger than the initial ΔG.

**AN INCREASE IN TAXES**



Initially, the tax increase reduces consumption, and therefore E: so firms reduce output, and income falls toward a new equilibrium

**SOLVING FOR ΔY**

Equilibrium condition in changes

I and G are exogenous

$$\begin{aligned}
 \Delta Y &= \Delta C + \Delta I + \Delta G \\
 &= \Delta C \\
 &= MPC \times (\Delta Y - \Delta T)
 \end{aligned}$$

Solving for  $\Delta Y$ :

$$(1 - MPC) \times \Delta Y = -MPC \times \Delta T$$

Final result:

$$\Delta Y = \left( \frac{-MPC}{1 - MPC} \right) \times \Delta T$$

**THE TAX MULTIPLIER**

The change in income resulting from a \$1 increase in T is known as tax multiplier.

$$\frac{\Delta Y}{\Delta T} = \frac{-MPC}{1 - MPC}$$

If MPC = 0.8, then the tax multiplier equals

$$\frac{\Delta Y}{\Delta T} = \frac{-0.8}{1 - 0.8} = \frac{-0.8}{0.2} = -4$$

**P**

1. Tax multiplier is negative: When taxes increase, consumer spending decreases, leading to a reduction in income.

2. Tax multiplier is greater than one (in absolute value): Changes in taxes have a multiplier effect on income, meaning that the impact on income is larger than the initial change in taxes.

reduces consumer spending, which reduces income.

**absolute value):** A change in taxes has a multiplier effect on income, meaning that the impact on income is larger than the initial change in taxes.

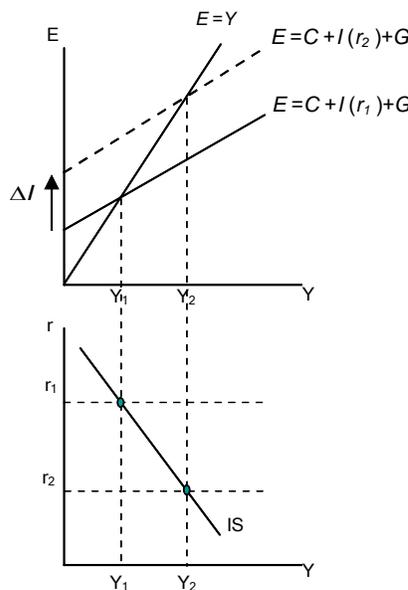
**spending multiplier:** Consumers save the most in spending from a tax cut is smaller than from an equal increase in G.

**IS CURVE**

A graph of all combinations of r and Y that result in goods market equilibrium is called IS curve i.e. Actual expenditure (output) = planned expenditure. The equation for the IS curve is:

$$Y = C(Y - \bar{T}) + I(r) + \bar{G}$$

**DERIVING THE IS CURVE**



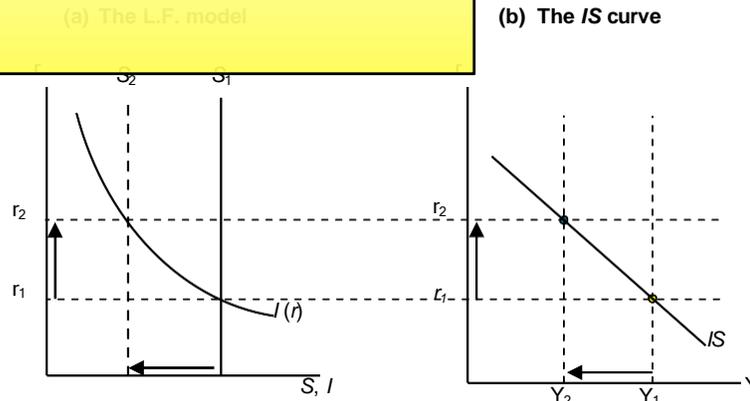
$$\downarrow r \Rightarrow \uparrow I \Rightarrow E \Rightarrow Y$$

IS-LM FRAMEWORK

IS curve is negatively sloped, showing the inverse relationship between the interest rate and output. A decrease in the interest rate motivates firms to increase investment spending, leading to higher total planned spending (E) and an increase in output to restore equilibrium in the goods market.

**IS CURVE AND THE LOANABLE FUNDS MODEL**

interest rate motivates firms to increase spending (E). To restore equilibrium in the goods market.

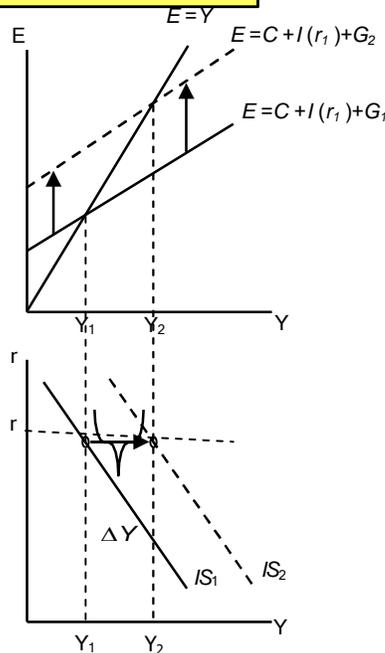


Fiscal policy, represented by changes in government spending (G) and taxes (T), can influence aggregate demand and output in the economy. Using the IS-LM model, we can analyze how fiscal policy shifts the IS curve.

**SHIFTING THE IS CURVE:  $\Delta G$**

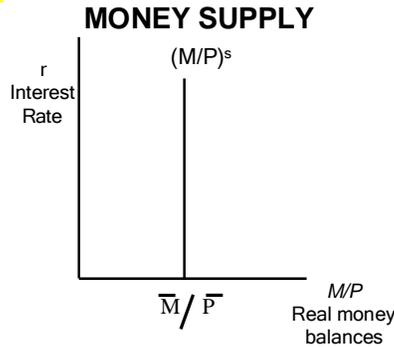
At any value of  $r$ ,  $\uparrow G \Rightarrow \uparrow E \Rightarrow \uparrow Y$ ...so the IS curve shifts to the right.

(G and T) can affect aggregate demand and output in the economy. We can see how fiscal policy shifts the IS



**THE THEORY OF LIQUIDITY PREFERENCE**

John Maynard Keynes presented a simple theory in which the interest rate is determined by money supply and money demand.

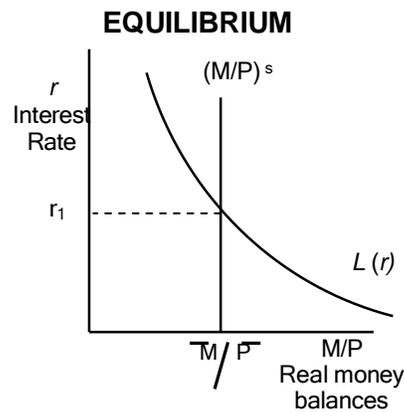
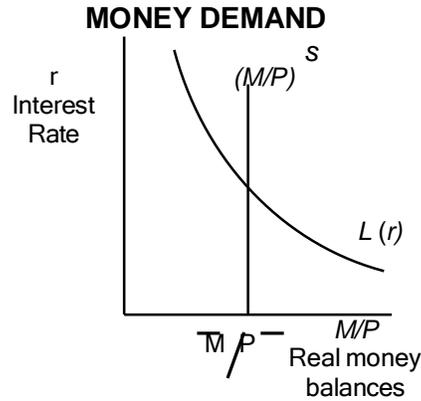


The supply of real money balances is fixed:

$$(M/P)^s = \bar{M}/\bar{P}$$

Demand for real money balances:

$$(M/P)^d = L(r)$$

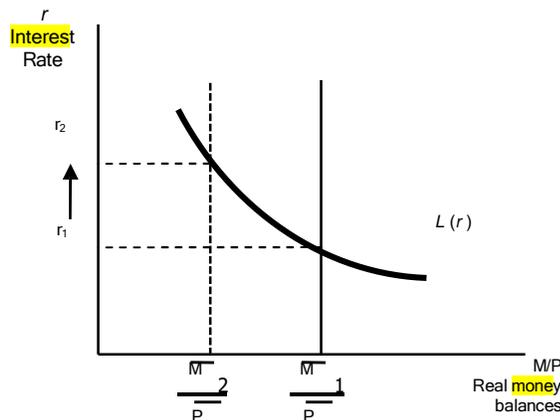


The interest rate adjusts to equate the supply and demand for money:

$$\bar{M}/\bar{P} = L(r)$$

**HOW CENTRAL BANK RAISES THE INTEREST RATE**

To increase  $r$ , Central Bank reduces  $M$ .



**LM CURVE**

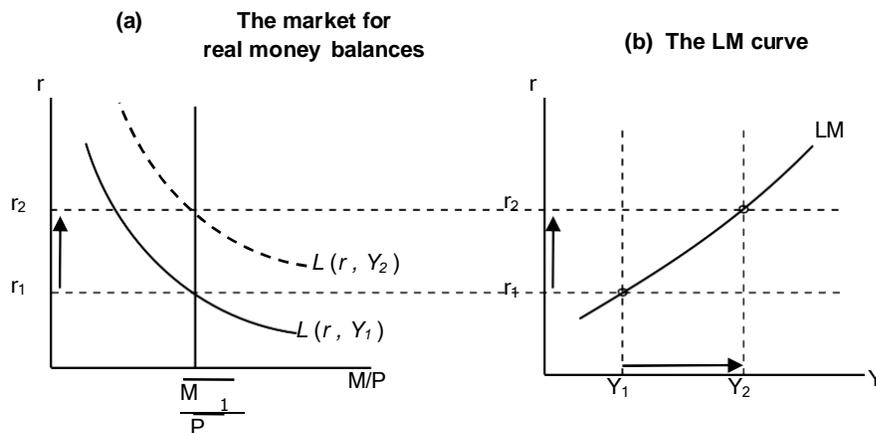
Now let's put  $Y$  back into the money demand function:

$$\left(\frac{M}{P}\right)^d = L(r, Y)$$

The LM curve is a graph of all combinations of  $r$  and  $Y$  that equate the supply and demand for real money balances. The equation for the LM curve is:

$$\bar{M} / \bar{P} = L(r, Y)$$

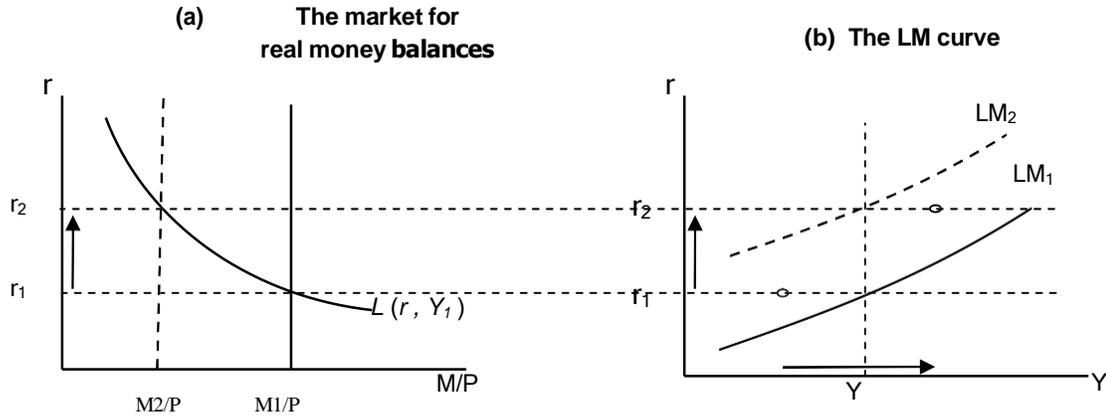
**DERIVING THE LM CURVE**



**LM CURVE'S SLOPE**

The LM curve is positively sloped. An increase in income raises money demand. Since the supply of real balances is fixed, there is now excess demand in the money market at the initial interest rate. The interest rate must rise to restore equilibrium in the money market.

**HOW  $\Delta M$  SHIFTS THE LM CURVE**



**SHIFTING THE LM CURVE**

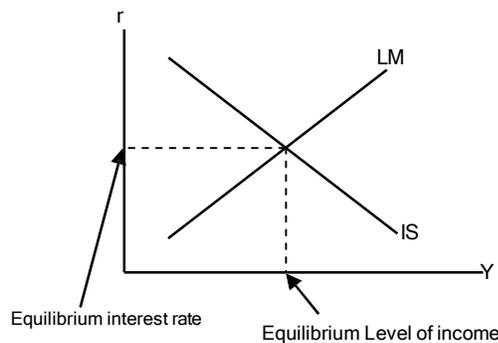
**Exercise Question:** Suppose a wave of credit card fraud causes consumers to use cash more frequently in transactions. Use the Liquidity Preference model to show how these events shift the LM curve.

**THE SHORT-RUN EQUILIBRIUM**

The short-run equilibrium is the combination of  $r$  and  $Y$  that simultaneously satisfies the equilibrium conditions in the goods & money markets:

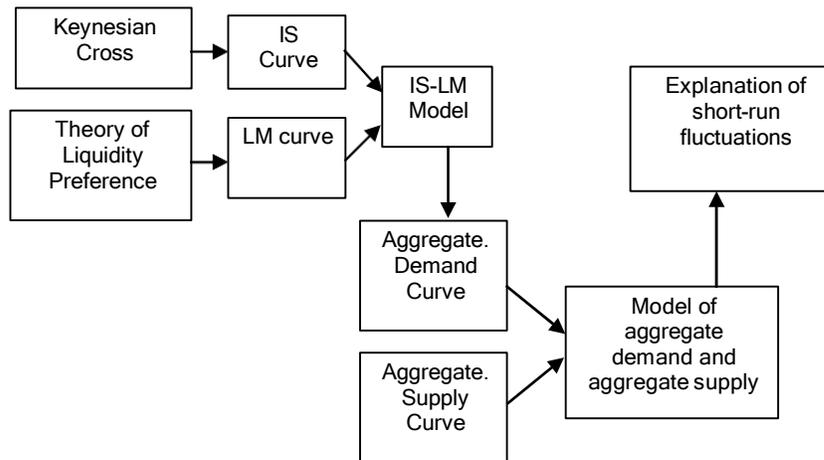
$$Y = C(Y - T) + I(r) + \bar{G}$$

$$\bar{M}/\bar{P} = L(r, Y)$$



**IS-LM FRAMEWORK (CONTINUED)**

**THE BIG PICTURE**



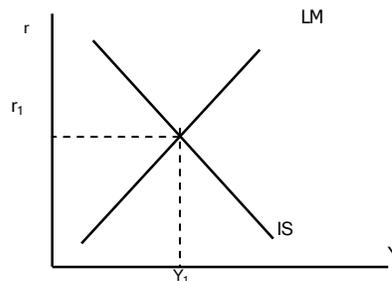
**EQUILIBRIUM IN THE IS-LM MODEL**

The **IS curve represents equilibrium in the goods market.**

$$Y = C(Y - \bar{T}) + I(r) + \bar{G}$$

The **LM curve represents money market equilibrium**

$$\bar{M} / \bar{P} = L(r, Y)$$

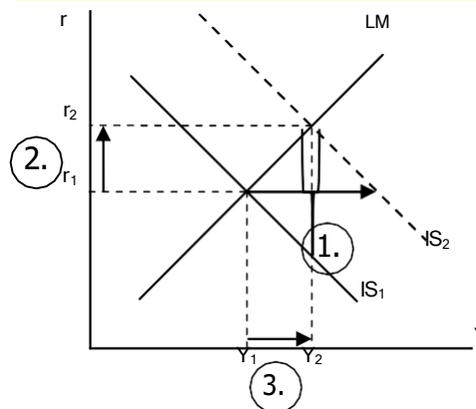


The intersection determines the unique combination of Y and r that satisfies equilibrium in both markets.

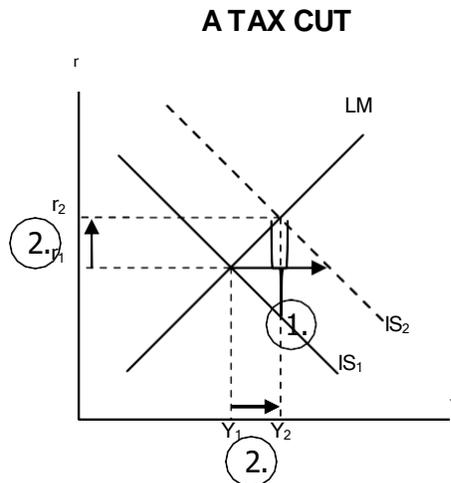
**POLICY ANALYSIS WITH THE IS-LM MODEL**

**Policymakers can affect macroeconomic variables with fiscal policy:** G and/or T and **monetary policy:** M. We can use the IS-LM model to analyze the effects of these policies.

**AN INCREASE IN GOVERNMENT PURCHASES**



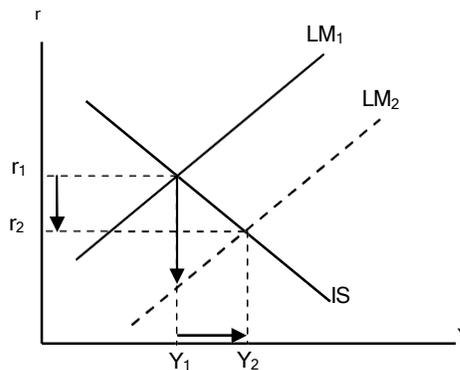
1. IS curve shifts right by  $\frac{1}{(1-MPC)} \Delta G$ , causing output & income to rise.
2. This raises money demand, causing the interest rate to rise.
3. Which reduces investment, so the final increase in Y is smaller than  $\frac{1}{(1-MPC)} \Delta G$ .



Because consumers save  $(1-MPC)$  of the tax cut, the initial boost in spending is smaller for  $\Delta T$  than for an equal  $\Delta G$ ... and the IS curve shifts by

1.  $\frac{1}{(1-MPC)} \Delta T$
2. So the effects on r and Y are smaller for a  $\Delta T$  than for an equal  $\Delta G$ .

**MONETARY POLICY: AN INCREASE IN M**



1.  $\Delta M > 0$  shifts the LM curve down (or to the right).
2. Causing the interest rate to fall.
3. This increases investment, causing output & income to rise.

**INTERACTION BETWEEN MONETARY & FISCAL POLICY**

**Model:** monetary & fiscal policy variables (M, G and T) are exogenous.

**Real world:** Monetary policymakers may adjust M in response to changes in fiscal policy, or vice versa. Such interaction may alter the impact of the original policy change.

**CENTRAL BANK'S RESPONSE TO  $\Delta G > 0$**

Suppose Government increases G. Possible central bank responses are:

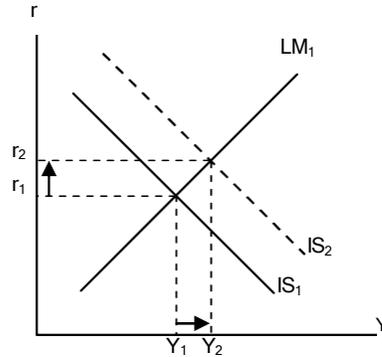
1. Hold M constant
2. Hold r constant

**3. Hold Y constant**

In each case, the effects of the  $\Delta G$  are different:

**RESPONSE 1: HOLD M CONSTANT**

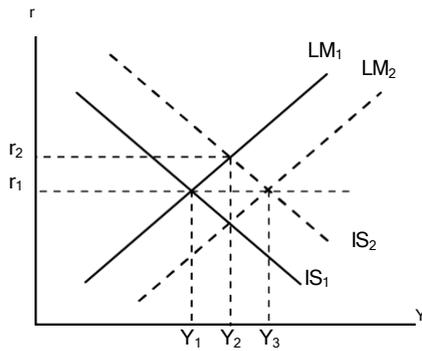
If Government raises G, the IS curve shifts right. If central bank holds M constant, then LM curve doesn't shift.



Results:  $\Delta Y = Y_2 - Y_1$        $\Delta r = r_2 - r_1$

**RESPONSE 2: HOLD r CONSTANT**

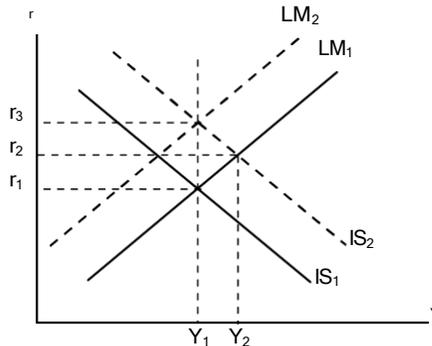
If Government raises G, the IS curve shifts right. To keep r constant, central bank increases M, to shift the LM curve right.



Results:  $\Delta Y = Y_3 - Y_1$        $\Delta r = 0$

**RESPONSE 3: HOLD Y CONSTANT**

If Government raises G, the IS curve shifts right. To keep Y constant, central Bank reduces M to shift LM curve left.



Results:  $\Delta Y = 0$        $\Delta r = r_3 - r_1$

**SHOCKS IN THE IS-LM MODEL**

**IS SHOCKS:** exogenous changes in the demand for goods & services.

**Examples:**

- Stock market boom or crash,  $\Rightarrow$  change in households' wealth,  $\Rightarrow \Delta C$
- Change in business or consumer confidence or expectations  $\Rightarrow \Delta I$  and/or  $\Delta C$

**LM SHOCKS:** exogenous changes in the demand for money.

**Examples:**

- A wave of credit card fraud increases demand for money
- More ATMs or the Internet reduce money demand

**Exercise Questions:**

Use the IS-LM model to analyze the effects of:

- A boom in the stock market makes consumers wealthier.
- After a wave of credit card fraud, consumers use cash more frequently in transactions.

For each shock,

- Use the IS-LM diagram to show the effects of the shock on  $Y$  and  $r$ .
- Determine what happens to  $C$ ,  $I$ , and the unemployment rate.

**WHAT IS THE CENTRAL BANK'S POLICY INSTRUMENT?**

What the newspaper says: "The central bank lowered interest rates by one-half point today".  
 What actually happened: The central bank conducted expansionary monetary policy to shift the LM curve to the right until the interest rate fell 0.5 points. The central bank targets the discount rate: it announces a target value, and uses monetary policy to shift the LM curve as needed to attain its target rate.

**Why does the central bank target interest rates instead of the money supply?**

- a) They are easier to measure than the money supply
- b) The central bank might believe that LM shocks are more prevalent than IS shocks. If so, then targeting the interest rate stabilizes income better than targeting the money supply.

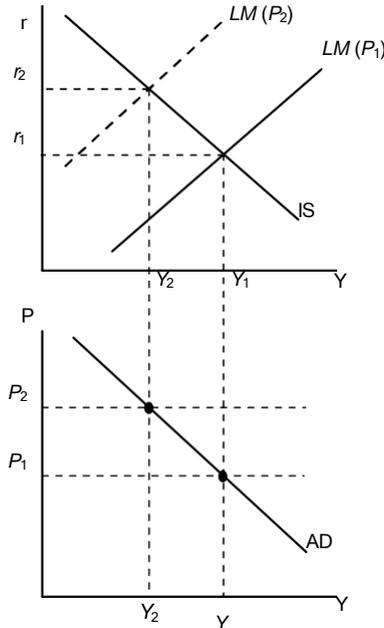
**IS-LM FRAMEWORK AND AGGREGATE DEMAND**

So far, we've been using the **IS-LM model to analyze the short run, when the price level is assumed fixed**. However, a change in  $P$  would shift the  $LM$  curve and therefore affect  $Y$ . The aggregate demand curve captures this relationship between  $P$  and  $Y$ .

**DERIVING THE AD CURVE**

Intuition for slope of AD curve:

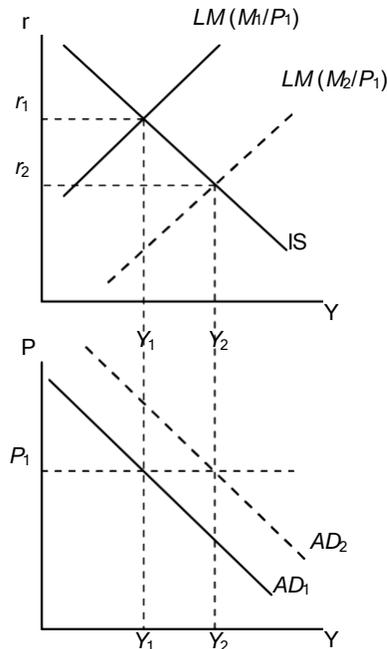
$P \Rightarrow \downarrow(M/P) \Rightarrow LM \text{ shifts left} \Rightarrow r \Rightarrow \downarrow I \Rightarrow \downarrow Y$



**MONETARY POLICY AND THE AD CURVE**

The central bank can increase aggregate demand:

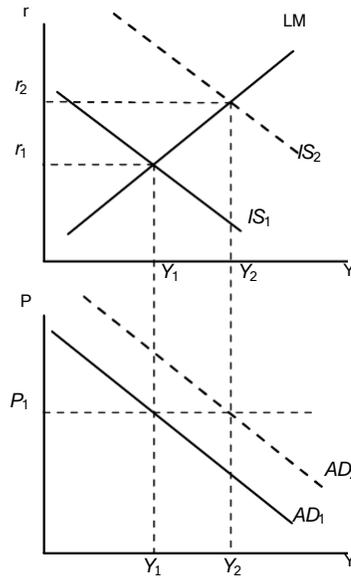
$M \Rightarrow LM \text{ shifts right} \Rightarrow \downarrow r \Rightarrow I \Rightarrow Y \text{ at each value of } P.$



**FISCAL POLICY AND THE AD CURVE**

Expansionary fiscal policy (G and/or ↓T) increases aggregate demand:

↓T ⇒ C ⇒ IS shifts right ⇒ Y at each value of P.



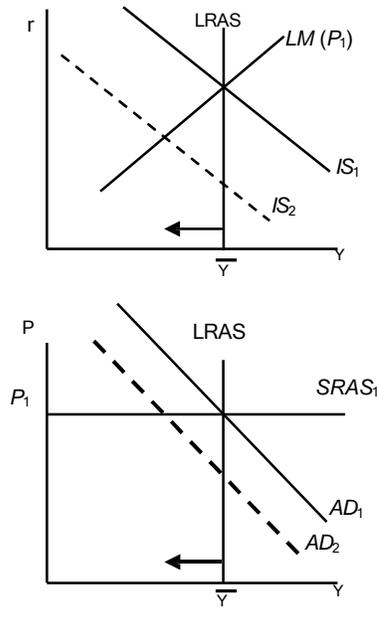
**IS-LM AND AD-AS IN THE SHORT RUN & LONG RUN**

**Recall:** The force that moves the economy from the short run to the long run is the gradual adjustment of prices.

In the short-run equilibrium, if	Then over time, the price level will
$Y > \bar{Y}$	Rise
$Y < \bar{Y}$	Fall
$Y = \bar{Y}$	Remain constant

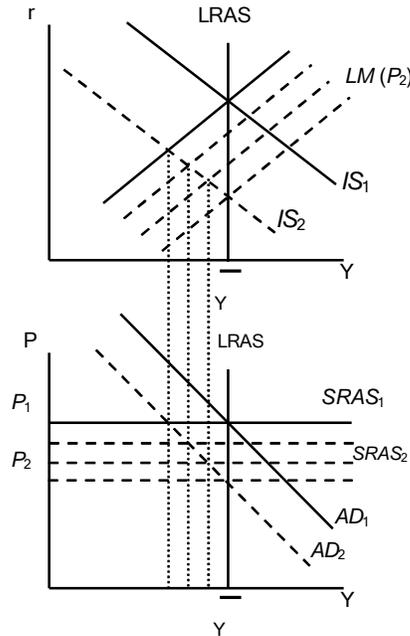
**THE SR AND LR EFFECTS OF AN IS SHOCK**

A negative IS shock shifts IS and AD left, causing Y to fall.

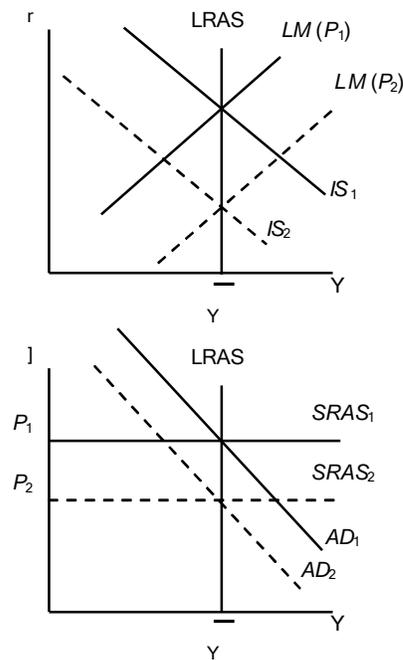


In the new short-run equilibrium,  $Y < \bar{Y}$ .

Over time,  $P$  gradually falls, which causes  $SRAS$  to move down,  $M/P$  to increase, which causes  $LM$  to move down.



This process continues until economy reaches a long-run equilibrium with  $Y = \bar{Y}$ .



**SHORT RUN IMPACTS**

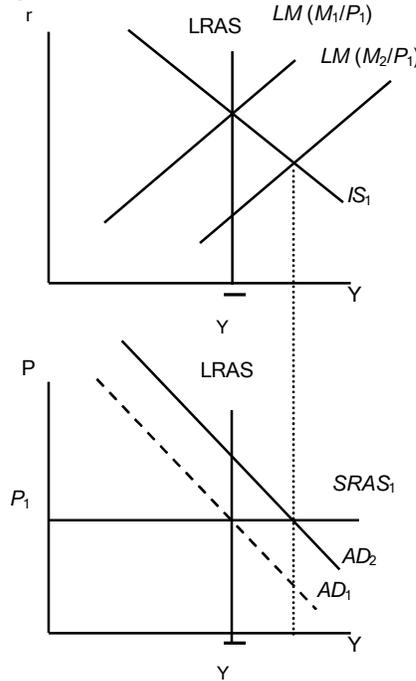
- Y     +, because Y moved.
- P     0, because prices are sticky in the SR.
- r     +, because a  $+\Delta Y$  leads to a rise in  $r$  as  $IS$  slides along the  $LM$  curve.
- C     +, because a  $+\Delta Y$  increases the level of consumption ( $C=C(Y-T)$ ).
- I     -, since  $r$  increased, the level of investment decreased.

**LONG RUN IMPACTS**

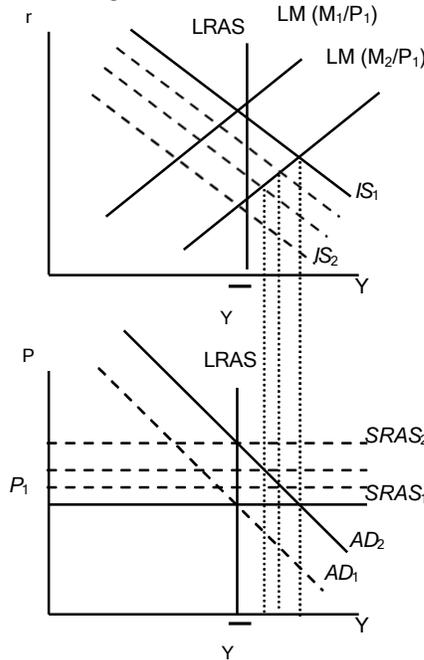
- Y = 0, because rising P shifts LM to left, returning Y to Y\* as required by long-run LRAS.
- P = +, in order to eliminate the excess demand at P<sub>0</sub>.
- r = +, reflecting the leftward shift in LM due to + ΔP.
- C = 0, since both Y and T are back to their initial levels (C=C(Y-T)).
- I = --, since r has risen even more due to the + ΔP.

**ANALYZE SR & LR EFFECTS OF ΔM**

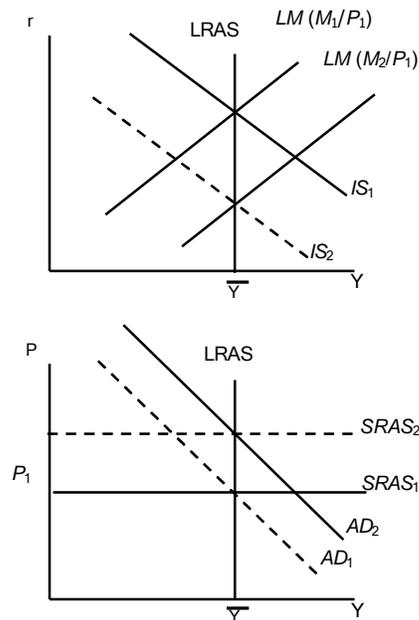
We have IS-LM and AD-AS diagrams as shown here. Suppose central bank increases M.



The Graph below shows the Short run effects of the change in M and what happens in the transition from the short run to the long run.



The new long-run equilibrium values of the endogenous variables as compared to their initial values



### SHORT RUN IMPACTS

Y +, because Y moved.

P 0, because prices are sticky in the SR.

r -, because a  $+\Delta Y$  leads to a decrease in  $r$  as LM slides along the IS curve.

C +, because a  $+\Delta Y$  increases the level of consumption ( $C=C(Y-T)$ ).

I +, since  $r$  decreased, the level of investment increased.

### LONG RUN IMPACTS

Y 0, because rising  $P$  shifts LM to left, returning  $Y$  to  $Y^*$  as required by long-run LRAS.

P +, in order to eliminate the excess demand at  $P_0$ .

r 0, reflecting the leftward shift in LM due to  $+\Delta P$  restoring  $r$  to its original level.

C 0, since both  $Y$  and  $T$  are back to their initial levels ( $C=C(Y-T)$ ).

I 0, since  $Y$  or  $r$  has not changed.

Notice that the only LR impact of an increase in the money supply was an increase in the price level.

**THE MUNDELL-FLEMING MODEL**

The Mundell-Fleming model portrays the relationship between the nominal exchange rate and the economy output. It is an extension of IS-LM model. Key assumption of this model is the small open economy with perfect capital mobility.

$$r = r^* \text{ (given)}$$

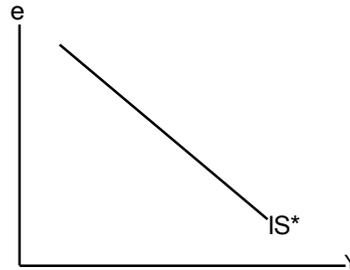
**IS\* CURVE: GOODS MARKET EQUILIBRIUM**

Goods market equilibrium-the IS\* curve:

$$Y = C ( Y - T ) + I ( r^* ) + G + N X ( e )$$

Where: e = nominal exchange rate = foreign currency per unit of domestic currency (e.g. 110 yen per dollar). The IS\* curve is drawn for a given value of r\*. Intuition for the slope:

$$\downarrow e \Rightarrow \uparrow NX \Rightarrow \uparrow Y$$

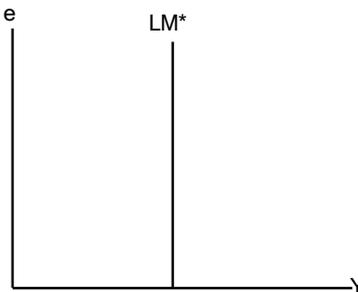


**LM\* CURVE: MONEY MARKET EQUILIBRIUM**

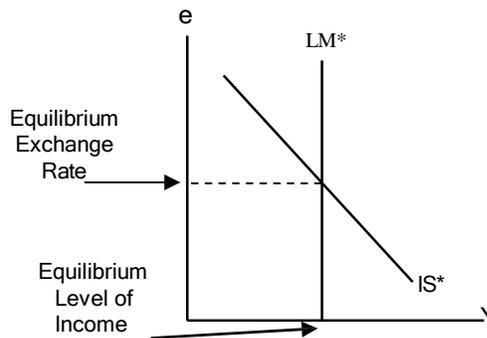
The LM\* curve equation is:

$$M / P = L ( r^* , Y )$$

LM\* curve is drawn for a given value of r\*. it is vertical because given r\*, there is only one value of Y that equates money demand with supply, regardless of e.



**EQUILIBRIUM IN THE MUNDELL-FLEMING MODEL**



**FLOATING**

In a system economic domestic for trade policy

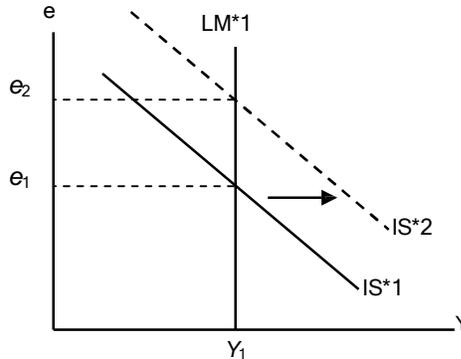
*Floating Exchange Rate System:*  
 - Exchange rate fluctuates based on market forces.  
 - Fiscal policy can be more flexible, with the government adjusting taxes and spending to influence the economy.  
 - Central banks have independence in conducting monetary policy using interest rates and open market operations.

uate in response to changing rates, the central bank trades consider fiscal, monetary, and fixed exchange rate system.

**FISCAL PO**  
 $Y =$

$$M/P = L(r^*, Y)$$

At any given value of  $e$ , a fiscal expansion increases  $Y$ , shifting  $IS^*$  to the right.



Results:  $\Delta e > 0, \Delta Y = 0$

**L**

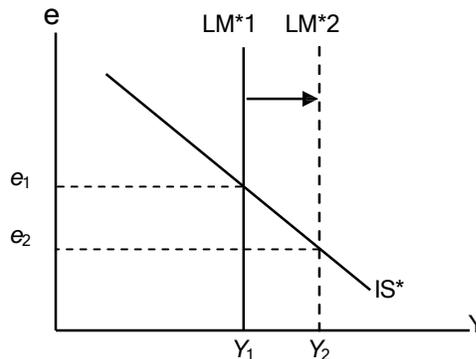
In a small open economy with perfect capital mobility, fiscal policy cannot influence real GDP.  
 In a closed economy, fiscal policy can crowd out investment by raising interest rates.  
 In a small open economy, fiscal policy crowds out net exports by causing the exchange rate to appreciate.

ability, fiscal policy is utterly incapable of investment by raising interest rates.  
 by causing the interest rate to rise.  
 net exports by causing the exchange rate to appreciate.

ability, fiscal policy is utterly incapable of investment by raising interest rates.  
 by causing the interest rate to rise.  
 net exports by causing the exchange rate to appreciate.

**MONETARY POLICY UNDER FLOATING EXCHANGE RATES**

An increase in  $M$  shifts  $LM^*$  right because  $Y$  must rise to restore equilibrium in the money market.



Results:  $\Delta e < 0, \Delta Y > 0$

**LESSONS ABOUT MONETARY POLICY**

Monetary policy affects output by affecting one (or more) of the components of aggregate demand:

M

-----  
Monetary policy influences output through aggregate demand components in closed and small open economies.

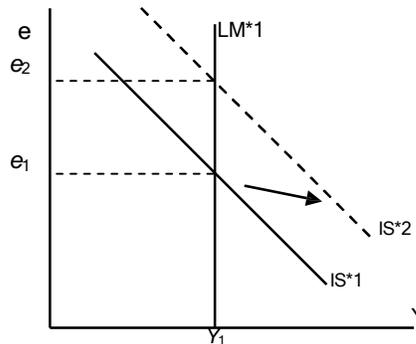
C  
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In a closed economy, increasing money supply (M) reduces interest rates ( $r$ ), boosting investments (I) and output (Y). In a small open economy, higher money supply (M) lowers the exchange rate ( $e$ ), increasing net exports (NX) and output (Y).

aggregate demand, it shifts demand from income and employment at home come at

THE MUNDELL-FLEMING MODEL (CONTINUED)

TRADE POLICY UNDER FLOATING EXCHANGE RATES

At any given value of  $e$ , a tariff or quota reduces imports, increases  $NX$ , and shifts  $IS^*$  to the right.



LESSONS ABOUT TRADE POLICY

Import restrictions cannot reduce a trade deficit. Even though  $NX$  is unchanged, there is less trade:

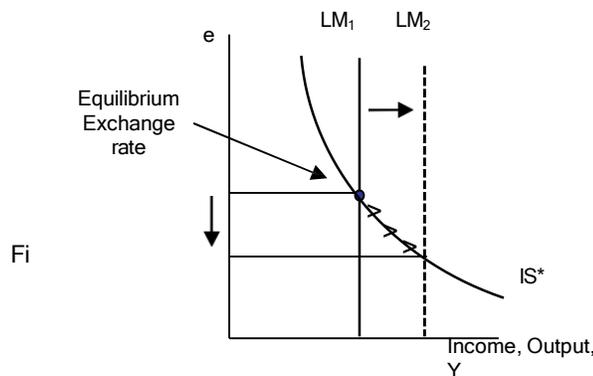
- The trade restriction reduces imports
- Exchange rate appreciation reduces exports

Less trade means fewer gains from trade. Import restrictions on specific products save jobs in the domestic industries that produce those products, but destroy jobs in export-producing sectors. Hence, import restrictions fail to increase total employment. Worse yet, import restrictions create “sectoral shifts,” which cause frictional unemployment.

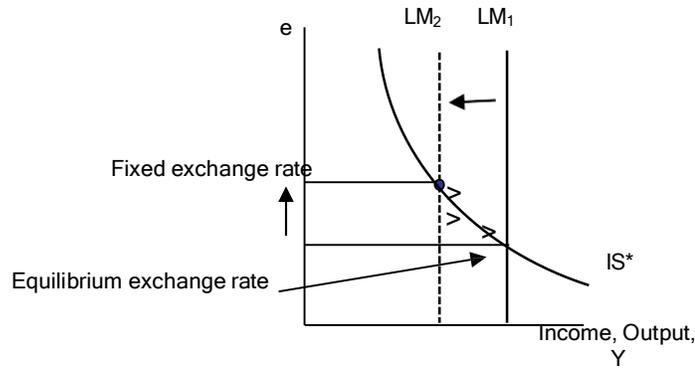
FIXED EXCHANGE RATES

Under a system of fixed exchange rates, the country’s central bank stands ready to buy or sell the domestic currency for foreign currency at a predetermined rate. In the context of the Mundell-Fleming model, the central bank shifts the  $LM^*$  curve as required to keep  $e$  at its pre-announced rate. This system fixes the nominal exchange rate. In the long run, when prices are flexible, the real exchange rate can move even if the nominal rate is fixed.

a. The Equilibrium exchange rate is Greater than the fixed exchange rate

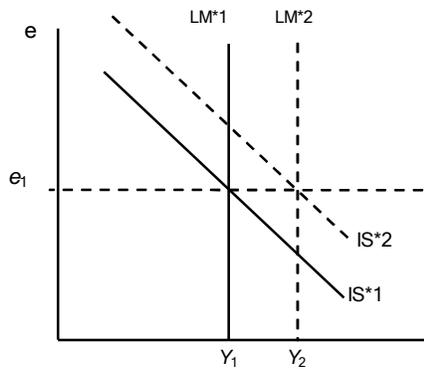


**b. The Equilibrium exchange rate is less than the fixed exchange rate**



**FISCAL POLICY UNDER FIXED EXCHANGE RATES**

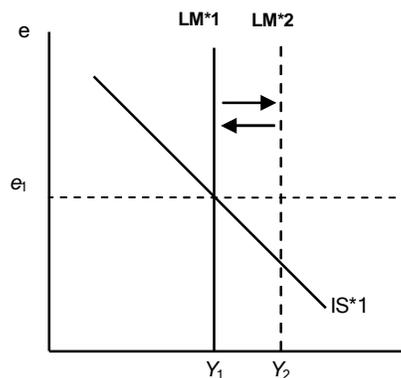
Under fixed exchange rates, a fiscal expansion would raise  $e$ . To keep  $e$  from rising, the central bank must sell domestic currency, which increases  $M$  and shifts  $LM^*$  right.



**Results:**  $\Delta e = 0, \Delta Y > 0$ . Under floating rates, fiscal policy ineffective at changing output. Under fixed rates, fiscal policy is very effective at changing output. LM shifts out!

**MONETARY POLICY UNDER FIXED EXCHANGE RATES**

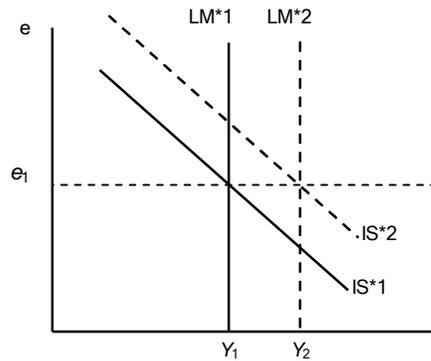
An increase in  $M$  would shift  $LM^*$  right and reduce  $e$ . To prevent the fall in  $e$ , the central bank must buy domestic currency, which reduces  $M$  and shifts  $LM^*$  back left.



**Results:**  $\Delta e = 0, \Delta Y = 0$ . Under floating rates, monetary policy is very effective at changing output. Under fixed rates, monetary policy cannot be used to affect output.

**TRADE POLICY UNDER FIXED EXCHANGE RATES**

A restriction on imports puts upward pressure on  $e$ . To keep  $e$  from rising, the central bank must sell domestic currency, which increases  $M$  and shifts  $LM^*$  right.



Results:  $\Delta e = 0, \Delta Y > 0$ . Under floating rates, import restrictions do not affect  $Y$  or  $NX$ . Under fixed rates, import restrictions increase  $Y$  and  $NX$ . But, these gains come at the expense of other countries, as the policy merely shifts demand from foreign to domestic goods

**M-F: SUMMARY OF POLICY EFFECTS**

Policy	Type of Exchange Rate Regime					
	Floating			Fixed		
	Impact on					
	Y	e	NX	Y	e	NX
Fiscal Expansion	0	□	□	□	0	0
Monetary Expansion	□	□	□	0	0	0
Import Restriction	0	□	0	□	0	□

**INTEREST-RATE DIFFERENTIALS**

There are two reasons why  $r$  may differ from  $r^*$ .

**1- Country risk:**

The risk that the country's borrowers will default on their loan repayments because of political or economic turmoil. Lenders require a higher interest rate to compensate them for this risk.

**2- Expected exchange rate changes:**

If a country's exchange rate is expected to fall, then its borrowers must pay a higher interest rate to compensate lenders for the expected currency depreciation.

**DIFFERENTIALS IN THE M-F MODEL**

$$r = r^* + \theta$$

Where  $\theta$  is a risk premium. Substitute the expression for  $r$  into the  $IS^*$  and  $LM^*$  equations:

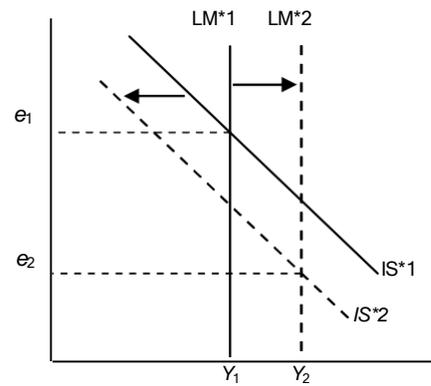
$$Y = C(Y - T) + I(r^* + \theta) + G + NX(e)$$

$$M/P = L(r^* + \theta, Y)$$

**THE EFFECTS OF AN INCREASE IN  $\theta$**

$IS^*$  shifts left, because  $\uparrow \theta \Rightarrow \uparrow r \Rightarrow \downarrow$

$LM^*$  shifts right, because  $\uparrow \theta \Rightarrow \uparrow r \Rightarrow \downarrow (M/P)_d$ , So  $Y$  must rise to restore money market equilibrium.



### THE EFFECTS OF AN INCREASE IN $\theta$

The fall in  $e$  is intuitive: An increase in country risk or an expected depreciation makes holding the country's currency less attractive.

**Note:** an **expected depreciation is a self-fulfilling prophecy**. The increase in  $Y$  occurs because the boost in  $NX$  (from the depreciation) is even greater than the fall in  $I$  (from the rise in  $r$ ).

**THE MUNDELL-FLEMING MODEL (CONTINUED) & THE THREE MODELS OF AGGREGATE SUPPLY**

**WHY INCOME MIGHT NOT RISE?**

- The central bank may try to prevent the depreciation by reducing the money supply.
- The depreciation might boost the price of imports enough to increase the price level (which would reduce the real money supply).
- Consumers might respond to the increased risk by holding more money.

Each of the above would shift LM\* leftward.

**THE SOUTH EAST ASIAN CRISIS**

	Exchange rate% change from 7/97 to 1/98	Stock market % change from 7/97 to 1/98	Nominal GDP% change 1997-98
Indonesia	-59.4%	-32.6%	-16.2%
Japan	-12.0%	-18.2%	-4.3%
Malaysia	-36.4%	-43.8%	-6.8%
Singapore	-15.6%	-36.0%	-0.1%
S. Korea	-47.5%	-21.9%	-7.3%
Taiwan	-14.6%	-19.7%	n.a.
Thailand	-48.3%	-25.6%	-1.2% (1996-97)
U.S.	n.a.	2.7%	2.3%

**FLOATING VS. FIXED EXCHANGE RATES**

**Argument for floating rates:**

Allows monetary policy to be used to pursue

**Arguments for fixed rates:**

Avoids uncertainty and volatility, making inter-

Disciplines monetary policy to prevent exces

-----

- Floating exchange rates allow countries to use monetary policy for economic goals like growth and low inflation. The currency's value adjusts to market forces, absorbing shocks.

- Fixed exchange rates offer stability, predictability, and ease in international transactions. They discipline monetary policy but require significant reserves and can face challenges if economic conditions diverge.

**MUNDELL-FLEMING AND THE AD CURVE**

Previously, we examined the M-F model with a fixed price level. To derive the AD curve, we now consider the impact of a change in P in the M-F model. We now write the M-F equations as:

$$(IS^*) \quad Y = C(Y - T) + I(r^*) + G + NX(\epsilon)$$

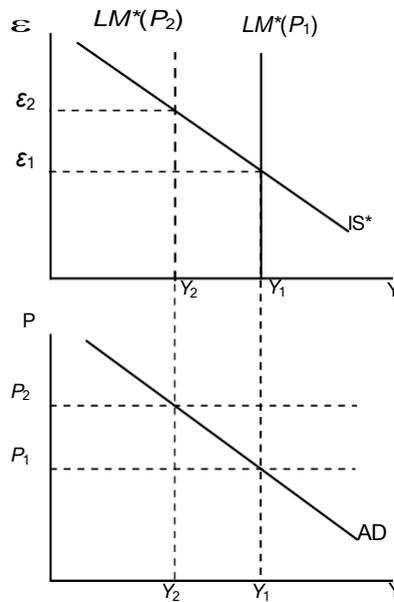
$$(LM^*) \quad M/P = L(r^*, Y)$$

(Earlier, we could write NX as a function of e because e and ε move in the same direction when P is fixed.)

**DERIVING THE AD CURVE**

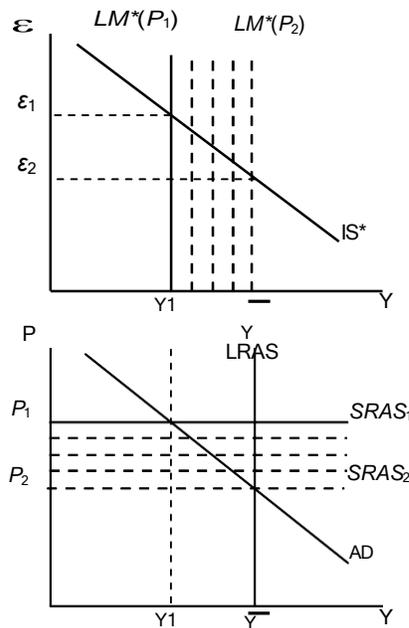
AD curve has negative slope because:

As P ⇒ ↓(M/P) ⇒ LM shifts left ⇒ ε ⇒ ↓NX ⇒ ↓Y



**FROM SHORT RUN TO THE LONG RUN**

If  $Y_1 < \bar{Y}$  then there is downward pressure on prices. Over time,  $P$  will move down, causing  $(M/P) \Rightarrow \epsilon \downarrow \Rightarrow NX \Rightarrow Y$



**LARGE: BETWEEN SMALL AND CLOSED**

Many countries - including the U.S. - are neither closed nor small open economies. A large open economy is in between the polar cases of closed & small open. Consider a monetary expansion:

Like in a closed economy,

$\Delta M > 0 \Rightarrow \downarrow r \Rightarrow \uparrow I$  (though not as much)

Like in a small open economy,

$\Delta M > 0 \Rightarrow \downarrow \epsilon \Rightarrow \uparrow NX$  (though not as much)

**THREE MODELS OF AGGREGATE SUPPLY**

1. The sticky-wage model
2. The imperfect-information model
3. The sticky-price model

All three models imply:

$$Y = \bar{Y} + \alpha (P - P^e)$$

Where:

- $\bar{Y}$  Aggregate output
- $Y$  Natural rate of output
- $\alpha$  a positive parameter
- $P$  the actual price level
- $P^e$  the expected price level

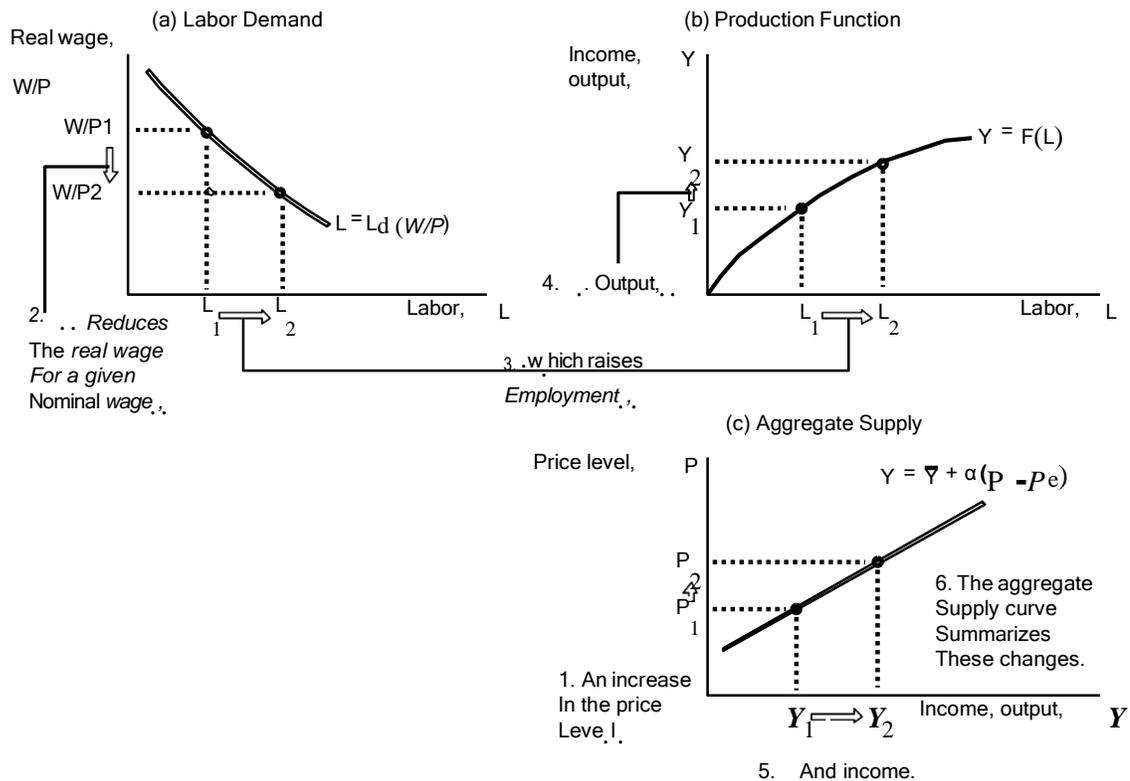
1- As kr ta

In the sticky-wage model, firms and workers set the nominal wage ( $W$ ) based on a target real wage ( $\omega$ ) and their expectation of future prices. Wages adjust slowly, leading to short-run effects on employment and output due to unexpected changes in the price level.

$$W = \omega \times P^e$$

$$\Rightarrow \frac{W}{P} = \omega \times \frac{P^e}{P}$$

If	Then
$P = P^e$	Unemployment and output are at their natural rates
$P > P^e$	Real wage is less than its target, so firms hire more workers and output rises above its natural rate
$P < P^e$	Real wage exceeds its target, so firms hire fewer workers and output falls below its natural rate



This model implies that the real wage should be counter-cyclical, it should move in the opposite direction as output over the course of business cycles:

- In booms, when P typically rises, the real wage should fall.
- In recessions, when P typically falls, the real wage should rise.

This prediction does not come true in the real world:

THREE MODELS OF AGGREGATE SUPPLY (CONTINUED)

2- THE IMPERFECT-INFORMATION MODEL

Assumptions:

- All wages and prices perfectly flexible.
- All markets are clear.
- Each supplier produces one good, consumes many goods.
- Each supplier knows the nominal price of the good she produces, but does not know the overall price level.

Supply of each good depends on its relative price: the nominal price of the good divided by the overall price level. Supplier doesn't know price level at the time she makes her production decision, so uses the expected price level,  $P^e$ . Suppose  $P$  rises but  $P^e$  does not. Then supplier thinks her relative price has risen, so she produces more. With many producers thinking this way,  $Y$  will rise whenever  $P$  rises above  $P^e$ .

3- THE STICKY-PRICE MODEL

Reasons for sticky prices are as follows:

- Long-term contracts between firms and customers.
- Menu costs.
- Firms do not wish to annoy customers with frequent price changes.

Assumptions:

Firms set their own prices (e.g. as in monopolistic competition).  
An individual firm's desired price is

$$p = P + a (Y - \bar{Y})$$

Where  $a > 0$ .

Suppose two types of firms:

- Firms with flexible prices, set prices as above
- Firms with sticky prices, must set their price before they know how  $P$  and  $Y$  will turn out:

$$p = P^e + a (Y^e - \bar{Y}^e)$$

Assume firms with sticky prices expect that output will equal its natural rate. Then,

$$p = P^e$$

To derive the aggregate supply curve, we first find an expression for the overall price level. Let  $s$  denote the fraction of firms with sticky prices. Then, we can write the overall price level as

$$P = s P^e + (1 - s) [P + a (Y - \bar{Y})]$$

Price set by sticky price firm
Price set by flexible price firm

Subtract  $(1-s)P$  from both sides:

$$sP = sP^e + (1 - s)[a(Y - \bar{Y})]$$

Divide both sides by  $s$ :

$$P = P^e + \left[ \frac{(1 - s)a}{s} \right] (Y - \bar{Y})$$

High  $P^e \Rightarrow$  High  $P$ . If firms expect high prices, then firms who must set prices in advance will set them high. Other firms respond by setting high prices.

High  $Y \Rightarrow$  High  $P$ . When income is high; the demand for goods is high. Firms with flexible prices set high prices. The greater the fraction of flexible price firms, the smaller is  $s$  and the bigger is the effect of  $\Delta Y$  on  $P$ .

Finally, derive AS equation by solving for  $Y$ :

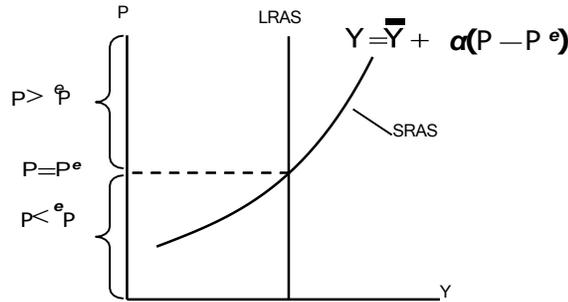
$$Y = \bar{Y} + \alpha (P - P^e),$$

where  $\alpha = \frac{s}{(1-s)a}$

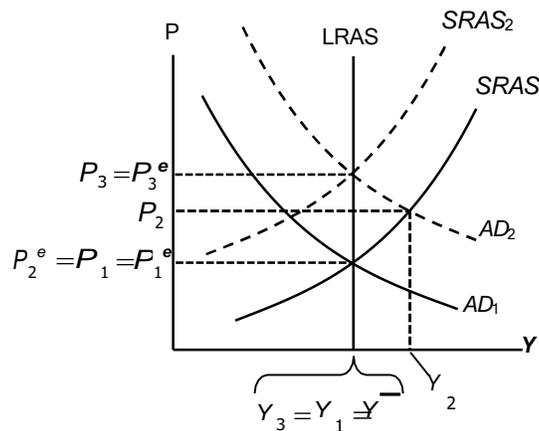
In contrast to the sticky-wage model, the sticky-price model implies a pro-cyclical real wage. Suppose aggregate output/income falls. Then, Firms see a fall in demand for their products. Firms with sticky prices reduce production, and hence reduce their demand for labor. The leftward shift in labor demand causes the real wage to fall.

**INFLATION, UNEMPLOYMENT, AND THE PHILLIPS CURVE**

Each of the three models of aggregate supply imply the relationship summarized by the SRAS curve & equation



Suppose a positive AD shock moves output above its natural rate and P above the level people had expected. Over time, Pe rises, SRAS shifts up, and output returns to its natural rate.



**INFLATION, UNEMPLOYMENT, AND THE PHILLIPS CURVE**

The Phillips curve states that  $\pi$  depends on Expected inflation,  $\pi^e$

**Cyclical unemployment:** the deviation of the actual rate of unemployment from the natural rate  
Supply shocks,  $v$

$$\pi = \pi^e - \beta(u - u^n) + v$$

Where  $\beta > 0$  is an exogenous constant.

**DERIVING THE PHILLIPS CURVE FROM SRAS**

The Phillips curve in its modern form states that the inflation rate depends on three forces:

- Expected inflation.
- The deviation of unemployment from the natural rate, called cyclical unemployment.
- Supply shocks.

We can derive the Phillips curve from our equation for aggregate supply.

$$(1) \quad Y = \bar{Y} + \alpha (P - P^e)$$

According to aggregate supply equation:

$$(2) \quad P = P^e + (1/\alpha) (Y - \bar{Y})$$

Here are the three steps. First, add to the right-hand side of the equation a supply shock  $v$  to represent exogenous events (such as change in world's oil prices) that alter the price level and shift the short run aggregate supply curve:

$$(3) \quad P = P^e + (1/\alpha)(Y - \bar{Y}) + v$$

Next, to go from the price level to inflation rates, subtract last year's price level  $P_{-1}$  from both sides of equation to obtain

$$(4) \quad (P - P_{-1}) = (P^e - P_{-1}) + (1/\alpha)(Y - \bar{Y}) + v$$

The term on the left hand side is the difference between current price level and last years price level, which is inflation. The term on the right hand side is the difference between the expected price level and last years price level, which is expected inflation. Therefore,

$$(5) \quad \pi = \pi^e + (1/\alpha)(Y - \bar{Y}) + v$$

Now to go from output to unemployment, recall Okun's law which gives a relationship between two variables. We can write this as

$$(6) \quad (1/\alpha)(Y - \bar{Y}) = -\beta(u - u^n)$$

Using this **Okun's law relationship**, we can substitute left-hand side value in equation number 5, and we obtain

$$(7) \quad \pi = \pi^e - \beta(u - u^n) + v$$

### THE PHILLIPS CURVE AND SRAS

$$\text{SRAS: } Y = \bar{Y} + \alpha(P - P^e)$$

$$\text{Phillips curve: } \pi = \pi^e - \beta(u - u^n) + v$$

#### SRAS curve:

Output is related to unexpected movements in the price level.

#### Phillips curve:

Unemployment is related to unexpected movements in the inflation rate.

### ADAPTIVE EXPECTATIONS

Adaptive expectations: an approach that assumes people form their expectations of future inflation based on recently observed inflation. A simple example:

Expected inflation = last year's actual inflation:

$$\pi^e = \pi_{-1}$$

Then, the Philips curve becomes:

$$\pi = \pi_{-1} - \beta(u - u^n) + v$$

### INFLATION INERTIA

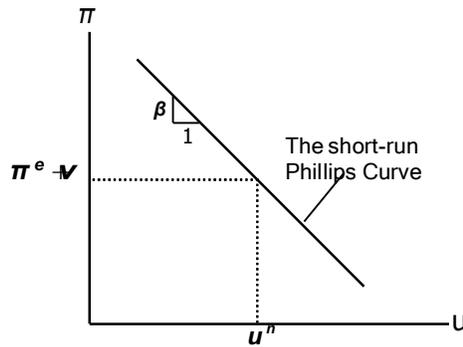
- In this form, the Phillips curve implies that inflation has inertia:
- In the absence of supply shocks or cyclical unemployment, inflation will continue indefinitely at its current rate.
- Past inflation influences expectations of current inflation, which in turn influences the wages & prices that people set.

**TWO CAUSES OF RISING & FALLING INFLATION**

- **Cost-push inflation:** inflation resulting from supply shocks. Adverse supply shocks typically raise production costs and induce firms to raise prices, “pushing” inflation up.
- **Demand-pull inflation:** inflation resulting from demand shocks. Positive shocks to aggregate demand cause unemployment to fall below its natural rate, which “pulls” the inflation rate up.

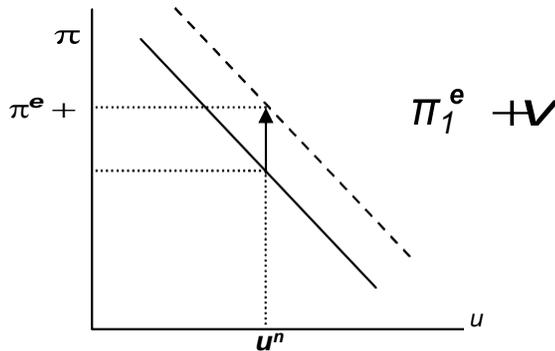
**GRAPHING THE PHILLIPS CURVE**

In the short run, policymakers face a trade-off between  $\pi$  and  $u$ .



**SHIFTING THE PHILLIPS CURVE**

People adjust their expectations over time, so the tradeoff only holds in the short run. e.g., an increase in  $\pi^e$  shifts the short-run P.C. upward.



**THE SACRIFICE RATIO**

To reduce inflation, policymakers can contract aggregate demand, causing unemployment to rise above the natural rate. The sacrifice ratio measures the percentage of a year’s real GDP that must be foregone to reduce inflation by 1 percentage point. Its estimates vary, but a typical one is 5.

Suppose policymakers wish to reduce inflation from 6 to 2 percent. If the sacrifice ratio is 5, then reducing inflation by 4 points requires a loss of  $4 \times 5 = 20$  percent of one year’s GDP.

This could be achieved several ways, e.g

- Reduce GDP by 20% for one year.
- Reduce GDP by 10% for each of two years.
- Reduce GDP by 5% for each of four years.

The cost of disinflation is lost GDP. One could use Okun’s law to translate this cost into unemployment.

## RATIONAL EXPECTATIONS

### Ways of modeling the formation of expectations:

- **Adaptive expectations:** People base their expectations of future inflation on recently observed inflation.
- **Rational expectations:** People base their expectations on all available information, including information about current & prospective future policies.

## PAINLESS DISINFLATION?

Proponents of rational expectations believe that the sacrifice ratio may be very small. Suppose  $u = u^n$  and  $\pi = \pi^e = 6\%$ , and suppose the central bank announces that it will do whatever is necessary to reduce inflation from 6 to 2 percent as soon as possible. If the announcement is credible, then  $\pi^e$  will fall, perhaps by the full 4 points. Then,  $\pi$  can fall without an increase in  $u$ .

## THE NATURAL RATE HYPOTHESIS

Our analysis of the costs of disinflation, and of economic fluctuations in the preceding chapters, is based on the natural rate hypothesis. Changes in aggregate demand affect output and employment only in the short run. In the long run, the economy returns to the levels of output, employment, and unemployment described by the classical model.

## AN ALTERNATIVE HYPOTHESIS: HYSTERESIS

**HYSTERESIS:** the long-lasting influence of history on variables such as the natural rate of unemployment. Negative shocks may increase  $u^n$ , so economy may not fully recover. The skills of cyclically unemployed workers deteriorate while unemployed, and they cannot find a job when the recession ends. Cyclically unemployed workers may lose their influence on wage-setting; insiders (employed workers) may then bargain for higher wages for themselves. Then, the cyclically unemployed “outsiders” may become structurally unemployed when the recession ends.

## GOVERNMENT DEBT

### GOVERNMENT DEBT AND THE ANNUAL BUDGET DEFICIT

When a government spends more than it collects in taxes, it borrows from the private sector to finance the budget deficit. The government debt is an accumulation of all past annual deficits.

#### COMPONENTS OF DOMESTIC DEBT

##### PERMANENT DEBT

- Market Loans
- Federal Government Bonds
- Income tax Bonds
- National Funds Bonds
- Federal investment Bonds
- Prize Bonds

##### FLOATING DEBT

- Treasury Bills
- Market Treasury Bills

##### UNFUNDED DEBTS

- Savings or Deposit Certificates
- Savings Account
- Postal Life insurance
- GP Fund

#### DOMESTIC DEBT OUTSTANDING

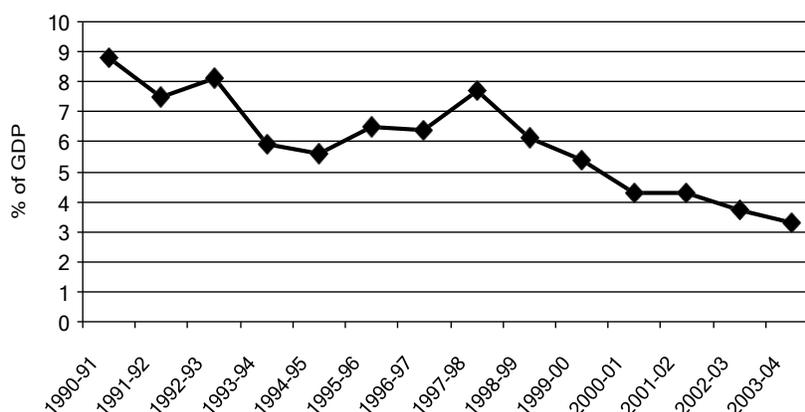
	Million Rupees		
	STOCK		Flow up to
	30-June-04	31-Jan-05	31-Jan-05
A: Permanent Debt	536,800	512,956	(23,844)
B: Floating Debt	542,943	611,648	68,704
C: Unfunded Debt	899,215	890,474	(8,741)
<b>Total (A + B + C)</b>	<b>1,978,958</b>	<b>2,015,078</b>	<b>36,120</b>

#### TRENDS IN PUBLIC DEBT

End June	Rs. Billions						
	1990	1995	2000	2001	2002	2003	2004
Debt payable in Rs	373.6	789.7	1575.9	1728.0	1715.2	1853.7	1921.4
% of GDP	42.8	42.3	41.5	41.5	39.1	38.4	35.2
Debt payable in Forex	427.6	872.5	1670.4	2025.8	1984.1	1891.3	1927.1
% of GDP	48.9	46.8	44.0	48.6	45.1	39.2	35.3
Total Public Debt	801.2	1662.2	3246.4	3753.8	3699.3	3745.0	3848.5
Grants			33.4	40.5	83.1	114.2	42.6
Net Public Debt	801.2	1662.2	3213.0	3713.3	3616.2	3630.8	3805.9
% of GDP	91.7	89.1	84.7	89.2	82.2	75.3	69.7

Source: Debt office, Ministry of Finance

### BUDGET DEFICIT OF PAKISTAN (as percentage of GDP)



#### PROBLEMS IN MEASUREMENT

Govt. Budget Deficit = Govt. Spending - Govt. Revenue  
= Amount of new debt

A meaningful deficit:

- Modifies the real value of outstanding public debt to reflect current inflation.
- Subtracts govt. assets from govt. debt.
- Includes hidden liabilities that currently escape detection in the accounting system.
- Calculates a cyclically-adjusted budget deficit.

#### INFLATION

Almost all economists agree that the government's indebtedness should be measured in real terms, not in nominal terms. The measured deficit should equal the change in the government's real debt, not the change in its nominal debt. However, the commonly measured budget deficit does not correct for inflation.

Suppose the real government debt is not changing. In other words, in real terms, the budget is balanced. In this case, the nominal debt must be rising at the rate of inflation. i.e.

$$\Delta D / D = \pi$$

Where,  $\pi$  is the inflation rate and  $D$  is the stock of government debt. This implies

$$\Delta D = \pi D$$

So by looking at the change in nominal debt  $\Delta D$ , a budget deficit of  $\pi D$  can be reported. Hence most economists believe that the reported budget deficit is overstated by the amount  $\pi D$ .

Another perspective: Govt. budget deficit = govt. Expenditure – Govt. Revenues

For correct measurement of budget deficit, the government expenditure should include only the real interest paid on the debt ( $rD$ ), not the nominal interest paid ( $iD$ ).

Since,  $i - r = \pi$

Budget deficit is overstated by  $\pi D$

**Example:**

In 1979, Budget deficit = \$28 billions,  $\pi = 8.6\%$ , Government debt = \$495 billion

Budget Deficit overstated,  $\pi D = 0.086 \times 495 = \$43$  billion

So,  $\$28 - \$43 = \$15$  billion surplus

#### CAPITAL ASSETS

An accurate assessment of government's budget deficit requires accounting for the govt.'s assets as well as liabilities. Particularly, when measuring govt.'s overall indebtedness, we should subtract government assets from government debt. So, Govt. budget deficit = change in debt –

**change in assets.** Individuals and firms treat assets and liabilities symmetrically. Borrowing to buy a house does not amount to budget deficit, because the increase in assets (house) is offset by increase in debt (lease rent) and thus, no change in net wealth. A budget procedure that accounts for assets as well liabilities is called capital budgeting, because it takes into account the changes in capital.

**For Example:**

The government sells some of its land or buildings and uses the proceeds to reduce the budget deficit.

- Under current budget procedure, the reported deficit would be lower.
- Under capital budgeting, reduction in debt would be offset by a reduction in assets.

Similarly, government borrowings to finance purchase of capital assets would not raise budget deficit.

**Problem with capital Budgeting**

It is hard to decide which government expenditures should count as capital expenditures.

**UNCOUNTED LIABILITIES**

- Measuring budget deficit may be misleading because it excludes some govt. liabilities.
- Pension of Govt. workers
- Social security system
- Although social security liabilities can be differentiated from government debt, yet the government can always choose not to repay all of its debt.

**THE BUSINESS CYCLE**

Changes occur automatically in response to a fluctuating economy.

**Example: Recession**

↓ Incomes ⇒ ↓ Personal Taxes

↓ Profits ⇒ ↓ Corporate Taxes

↓ Number of needy persons ⇒ ↑ G, Budget Deficit Increases

These automatic changes are not errors in measurement since government truly borrows in such situations. But this makes it difficult to use deficit to monitor changes in fiscal policy i.e. the deficit can either fall or rise either because Government has changed its policy or economy has changed direction. Cyclically adjusted (full employment) budget deficit reflects policy changes but not the current stage of the business cycle.

**GOVERNMENT DEBT (CONTINUED)**

**TRADITIONAL VIEW OF GOVT. DEBT**

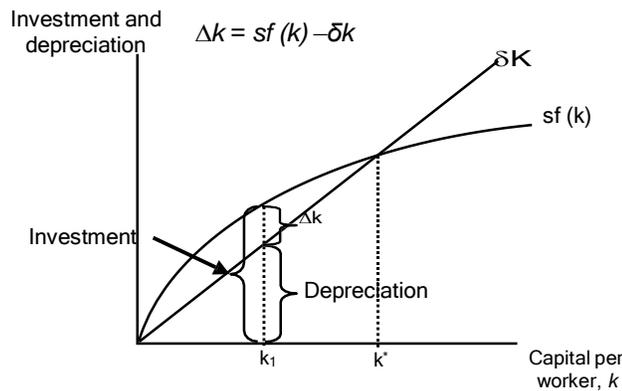
How would a tax cut and budget deficit affect the economy and the economic well-being of the country? A tax cut stimulates consumer spending and reduces national saving. The reduction in saving raises the interest rate, which crowds out investment. The Solow growth model shows that lower investment leads to a lower steady-state capital stock and lower output.

**SOLOW GROWTH MODEL**

Change in capital stock = investment - depreciation

$$\Delta k = i - \delta k$$

Since  $i = sf(k)$ , this becomes:  $\Delta k = s f(k) - \delta k$

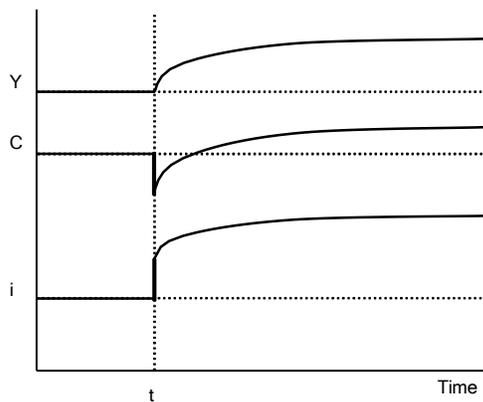


The economy will then have less capital than the Golden Rule steady-state which will mean lower consumption and lower economic well-being.

**STARTING WITH TOO LITTLE CAPITAL**

If  $K^* < K^*_{gold}$ , then increasing  $c^*$  requires an increase in  $s$ .

Future generations enjoy higher consumption, but the current one experiences an initial drop in consumption.

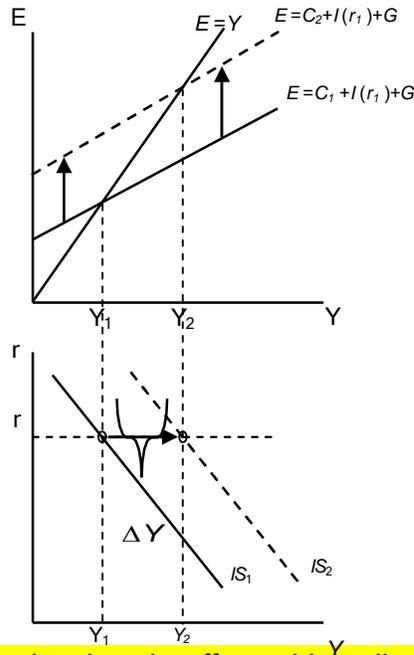


Then we analyze the short-run impact of the policy change via the IS-LM model.

**A TAX CUT**

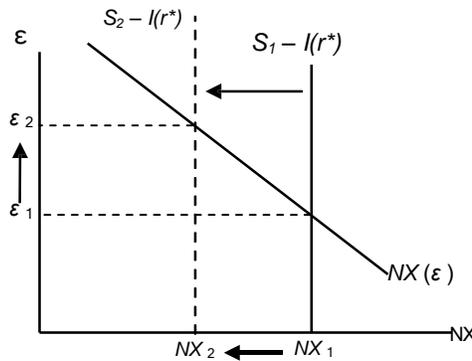
We Have  $C = C(Y - T)$ , at any value of  $r$ ,  $\downarrow T \Rightarrow \uparrow C \Rightarrow \uparrow E \Rightarrow \uparrow Y$

So the IS curve shifts to the right. The horizontal distance of the IS shift equals  $\Delta Y = MPC / (1 - MPC) \Delta T$ .



Next, we can see how international trade affects this policy change. When national saving falls, people borrow from abroad, causing a trade deficit. It also causes the local currency to appreciate.

**INTERNATIONAL TRADE**



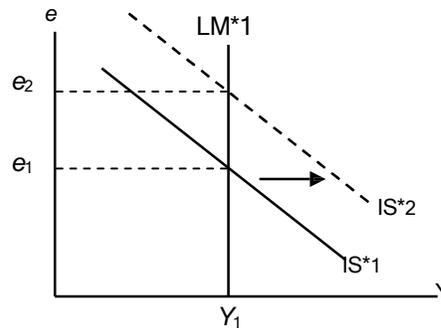
The Mundell-Fleming model shows that the appreciation and the resulting fall in net exports reduce the short-run expansionary effect of the fiscal change.

**MUNDELL-FLEMING MODEL**

$$Y = C(Y - T) + I(r^*) + G + NX(e)$$

$$M/P = L(r^*, Y)$$

At any given value of  $e$ , a fiscal expansion increases  $Y$ , shifting  $IS^*$  to the right. Results:  $\Delta e > 0$ ,  $\Delta Y = 0$ .



### THE RICARDIAN VIEW OF GOVERNMENT DEBT

Forward-looking consumers perceive that lower taxes now mean higher taxes later, leaving consumption unchanged. “Tax cuts are simply tax postponements.” When the government borrows to pay for its current spending (higher  $G$ ), rational consumers look ahead to the future taxes required to support this debt.

#### Another view:

- Govt. borrows Rs. 1,000 from a citizen to give him a Rs. 1,000 tax cut (similar to as giving him a Rs. 1,000 govt. bond as a gift)
- On one side the government owes him Rs. 1,000 plus interest. On the other side, he owes Rs. 1,000 plus interest.
- Overall no change in citizen’s wealth because the value of the bond is offset by the value of the future tax liability

#### General Principal (Ricardian equivalence)

- Government Debt is equivalent to future taxes
- If consumers are forward looking, future taxes are equivalent to current taxes
- So, financing govt. by debt is equivalent to financing it by taxes.

### CONSUMERS AND FUTURE TAXES

The essence of the Ricardian view is that when people choose their consumption, they rationally look ahead to the future taxes implied by government debt. But, how forward-looking are consumers? Defenders of the traditional view of government debt believe that the prospect of future taxes does not have as large an influence on current consumption as the Ricardian view assumes.

### MYOPIA

Ricardian view assumes that people are rational when making decisions. When the govt. borrows to pay for current spending, rational consumers look ahead to anticipate the future taxes required to support this debt.

Traditional view is that people are myopic, meaning that they see a decrease in taxes in such a way that their current consumption increases because of this new “wealth.” They don’t see that when expansionary fiscal policy is financed through bonds, they will just have to pay more taxes in the future since bonds are just tax-postponements.

### BORROWING CONSTRAINTS

The Ricardian view assumes that consumers base their spending not only on current but on their lifetime income, which includes both current and expected future income. Advocates of the traditional view argue that current consumption is more important than lifetime income for those consumers who face borrowing constraints, which are limits on how much an individual can borrow from financial institutions.

A person who wants to consume more than his current income must borrow. If he can’t borrow to finance his current consumption, his current income determines what he can consume, regardless of his future income. So, a debt-financed tax cut raises current income and thus

consumption, even though future income is lower. In essence, when a government cuts current taxes and raises future taxes, it is giving tax payers a loan.

**FUTURE GENERATIONS**

According to traditional view of government debt, consumers expect the implied future taxes to fall not of them but on future generations. This behavior raises the lifetime resources of the current generation as well as their consumption. In essence, the debt-financed tax cut stimulates the consumption because it gives the current generation the opportunity to consume at the expense of the next generation

**CONSUMPTION THEORIES**

**JOHN MAYNARD KEYNES AND THE CONSUMPTION FUNCTION**

The consumption function was central to Keynes' theory of economic fluctuations presented in The General Theory in 1936.

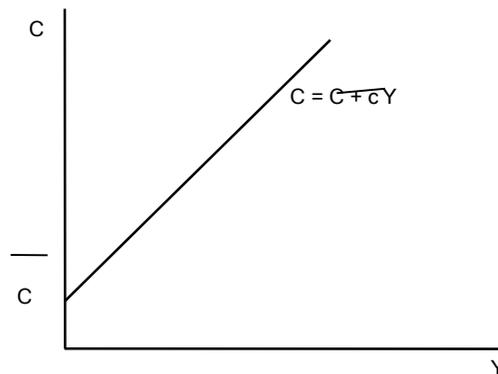
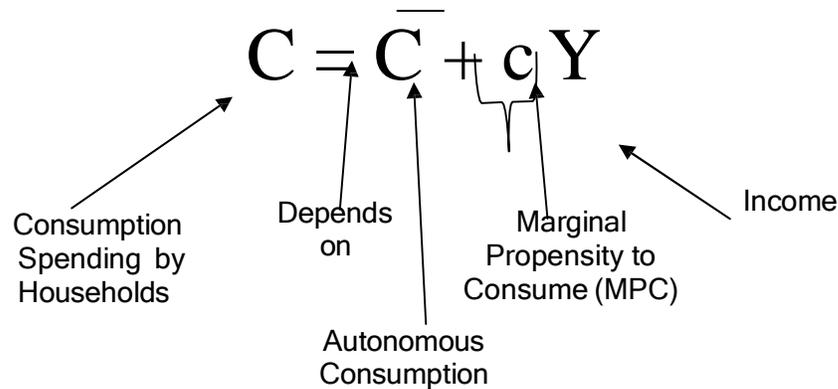
**K**-----  
 John Maynard Keynes' theory in "The General Theory" highlighted the consumption function's significance in economic fluctuations. His key points were:  
 1. MPC Conjecture: People consume part of extra income, saving the rest (MPC between 0 and 1).  
 2. APC Trend: As income rises, the proportion spent (APC) interest rate does not have an important role.

**propensity to consume**-- the amount e-- is between zero and one. He claimed every dollar of earned income, people will

**propensity to consume**-- the ratio of consumption

determinant of consumption and that the

**THE CONSUMPTION FUNCTION**

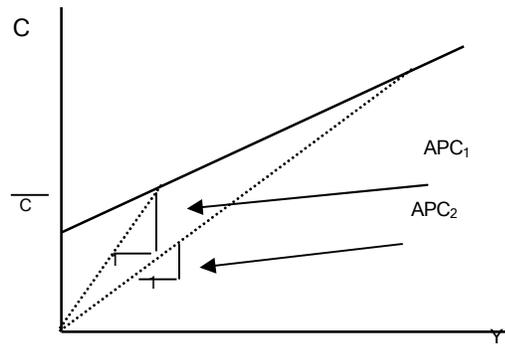


**This consumption function exhibits three properties that Keynes conjectured.**

1. The marginal propensity to consume  $c$  is between zero and one.
2. The average propensity to consume falls as income rises.
3. Consumption is determined by current income.

**AVERAGE PROPENSITY TO CONSUME**

$APC = C/Y = \bar{C}/Y + c$ , As  $Y$  rises,  $C/Y$  falls, and so the average propensity to consume  $C/Y$  falls. Notice that the interest rate is not included in this function.



### MARGINAL PROPENSITY TO CONSUME

To understand the marginal propensity to consume (MPC), consider a shopping scenario. A person who loves to shop probably has a large MPC, let's say (.99). This means that for every *extra* rupee he or she earns after tax deductions, he or she spends 99 paisas of it. The MPC measures the sensitivity of the change in one variable (C) with respect to a change in the other variable (Y).

### SECULAR STAGNATION AND SIMON KUZNETS

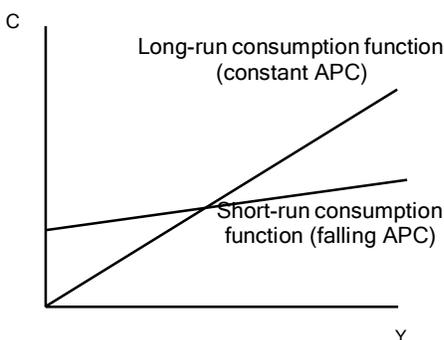
- During World War II, on the basis of Keynes' consumption function, economists predicted that the economy would experience what they called secular stagnation, a long depression of infinite duration-- unless fiscal policy was used to stimulate aggregate demand.
- It turned out that the end of the war did not throw the U.S. into another depression, but it did suggest that Keynes' conjecture that the average propensity to consume would fall as income rose appeared not to hold.
- Simon Kuznets constructed new aggregate data on consumption and investment dating back to 1869 and whose work would later earn a Nobel Prize.
- He discovered that the ratio of consumption to income was stable over time, despite large increases in income; again, Keynes' conjecture was called into question. This brings us to the puzzle.

### CONSUMPTION PUZZLE

The failure of the secular-stagnation hypothesis and the findings of Kuznets both indicated that the average propensity to consume is fairly constant over time. This presented a puzzle: why did Keynes' conjectures hold up well in the studies of household data and in the studies of short time-series, but fail when long time series were examined?

Studies of household data and short time-series found a relationship between consumption and income similar to the one Keynes conjectured-- this is called the short-run consumption function.

But, studies using long time-series found that the APC did not vary systematically with income--this relationship is called the long-run consumption function.



### IRVING FISHER AND INTERTEMPORAL CHOICE

The economist Irving Fisher developed the model with which economists analyze how rational, forward-looking consumers make intertemporal choices-- that is, choices involving different periods of time.

The model illuminates

- The constraints consumers face,
- The preferences they have, and
- How these constraints and preferences together determine their choices about consumption and saving.

When consumers are deciding how much to consume today versus how much to consume in the future, they face an intertemporal budget constraint, which measures the total resources available for consumption today and in the future.

### CONSUMER'S BUDGET CONSTRAINT

Consider the decision facing a consumer who lives for two periods (representing youth & age). He earns income  $Y_1$ ,  $Y_2$  and consumes  $C_1$ ,  $C_2$  in both periods respectively (adjusted for inflation). The savings in the first period will be

$$S = Y_1 - C_1$$

In the second period

$$C_2 = (1 + r) S + Y_2$$

Where  $r$  is the real interest rate. Remember  $S$  can represent either saving or borrowing and the equations hold in both cases.

- If  $C_1 < Y_1$  consumer is saving  $S > 0$
- If  $C_1 > Y_1$  consumer is borrowing  $S < 0$

Assume:  $r$  (borrowing) =  $r$  (saving)

Combining the two equations:

$$C_2 = (1 + r)(Y_1 - C_1) + Y_2$$

Rearranging

$$(1 + r)C_1 + C_2 = (1 + r)Y_1 + Y_2$$

Dividing both sides by  $1 + r$

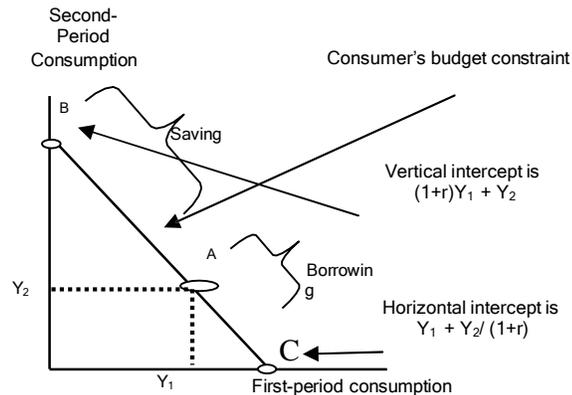
$$C_1 + \frac{C_2}{1 + r} = Y_1 + \frac{Y_2}{1 + r}$$

### So we can say that

- The consumer's budget constraint implies that if the interest rate is zero, the budget constraint shows that total consumption in the two periods equals total income in the two periods. In the usual case in which the interest rate is greater than zero, future consumption and future income are discounted by a factor of  $1 + r$ .
- This *discounting* arises from the interest earned on savings. Because the consumer earns interest on current income that is saved, future income is worth less than current income.

- Also, because future consumption is paid for out of savings that have earned interest, future consumption costs less than current consumption.
- The factor  $1/(1+r)$  is the price of second-period consumption measured in terms of first-period consumption; it is the amount of first-period consumption that the consumer must forgo to obtain 1 unit of second-period consumption.

Here are the combinations of first-period and second-period consumption the consumer can choose.



If he chooses a point between A and B, he consumes less than his income in the first period and saves the rest for the second period. If he chooses between A and C, he consumes more than his income in the first period and borrows to make up the difference.

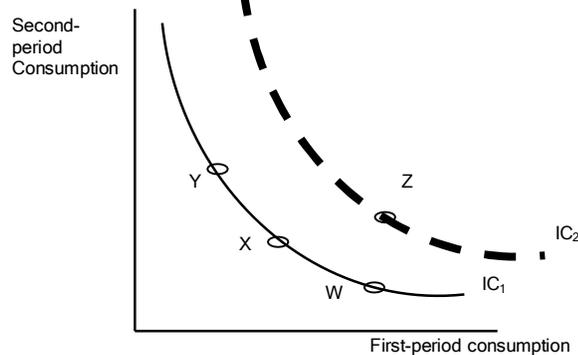
## CONSUMPTION THEORIES (CONTINUED)

### CONSUMER PREFERENCES

The consumer's preferences regarding consumption in the two periods can be represented by indifference curves.

An indifference curve shows the combination of first-period and second-period consumption that makes the consumer equally happy.

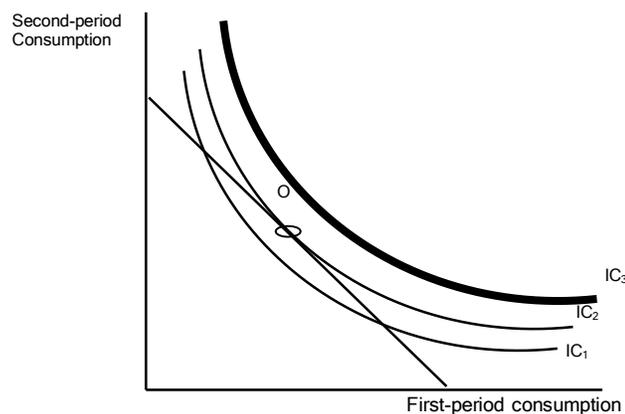
The slope at any point on the indifference curve shows how much second-period consumption the consumer requires in order to be compensated for a 1-unit reduction in first-period consumption. This slope is the marginal rate of substitution between first-period consumption and second-period consumption. It tells us the rate at which the consumer is willing to substitute second-period consumption for first-period consumption.



Higher indifference curves such as IC2 are preferred to lower ones such as IC1. The consumer is equally happy at points W, X, and Y, but prefers Z to all the others-- Point Z is on a higher indifference curve and is therefore not equally preferred to W, X and Y.

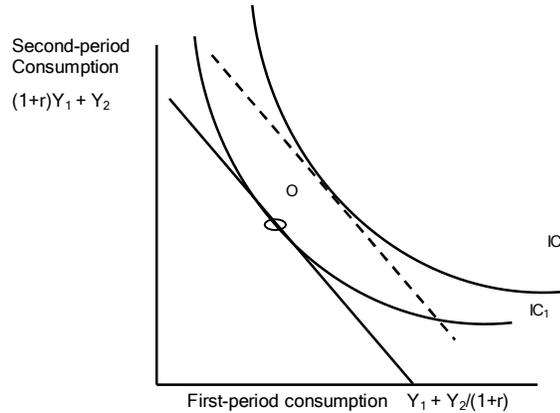
### OPTIMIZATION

The consumer achieves his highest (or optimal) level of satisfaction by choosing the point on the budget constraint that is on the highest indifference curve. At the optimum, the indifference curve is tangent to the budget constraint.



**HOW CHANGES IN INCOME AFFECT CONSUMPTION?**

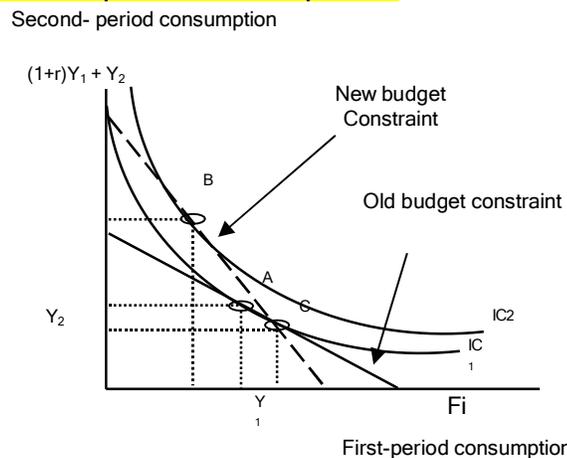
An increase in either first- or second-period income shifts the budget constraint outward. If consumption in period one and consumption in period two are both normal goods- those that are demanded more as income rises, this increase in income raises consumption in both periods.



**HOW CHANGES IN REAL INTEREST RATE AFFECT CONSUMPTION?**

Economists decompose the impact of an increase in the real interest rate on consumption into two effects: an income effect and a substitution effect.

1. The income effect is the change in consumption that results from the movement to a higher indifference curve.
2. The substitution effect is the change in consumption that results from the change in the relative price of consumption in the two periods.



An increase in the interest rate rotates the budget constraint around the point C, where C is (Y1, Y2). The higher interest rate reduces first period consumption (move to point A) and raises second-period consumption (move to point B). Irving Fisher’s Model shows that depending on the consumer preferences, changes in real interest rate could either raise or lower consumption. So, economic theory alone cannot predict how interest rate influences consumption. Therefore economists have studied the empirics of interest rate affecting the consumption and saving.

**SAVINGS AND THE REAL INTEREST RATE**

Data shows that there’s no apparent relationship between the two variables. Or, savings does not depend on interest rate. Economists claim that income and substitution effects of higher interest rates approximately cancel each other.

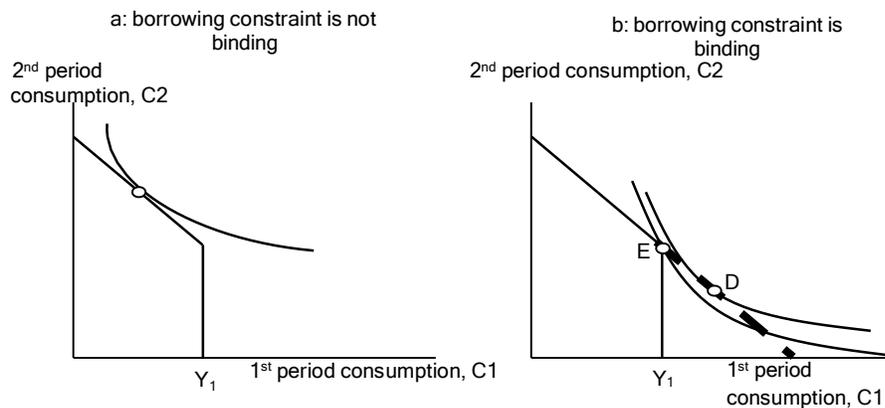
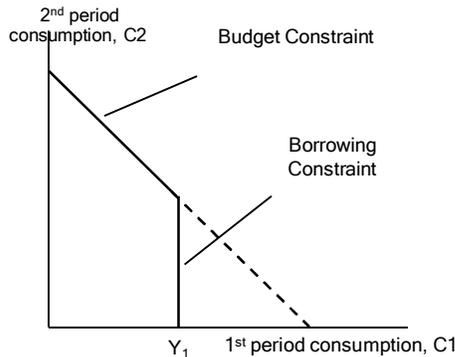
**CONSTRAINTS ON BORROWINGS**

The inability to borrow prevents current consumption from exceeding current income. A constraint on borrowing can therefore be expressed as  $C_1 \leq Y_1$ . This inequality states that consumption in period one must be less than or equal to income in period one. This additional constraint on the consumer is called a borrowing constraint, or sometimes, a liquidity constraint.

**Conclusions:**

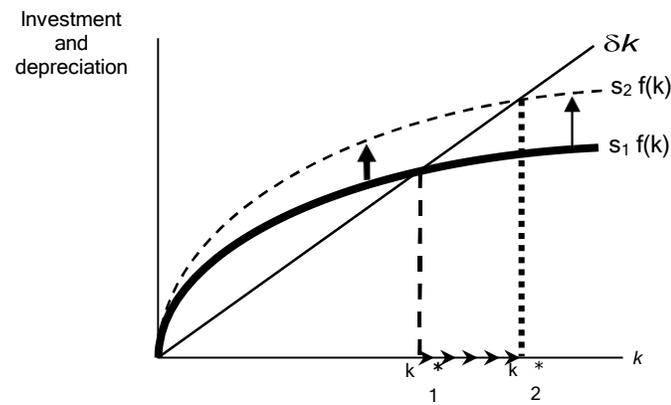
The analysis of borrowing leads us to conclude that there are two consumption functions.

- For some consumers, the borrowing constraint is not binding, and consumption in both periods depends on the present value of lifetime income.
- For other consumers, the borrowing constraint binds. Hence, for those consumers who would like to borrow but cannot, consumption depends only on current income.
- If the consumer cannot borrow, he faces the additional constraint that 1<sup>st</sup> period consumption cannot exceed 1<sup>st</sup> period income.



**HIGH JAPANESE SAVINGS RATE**

Japan has one of the world's highest savings rate. On one hand, many economists believe that this is a key to the rapid growth Japan experienced in the decades after World War II, the Solow growth model also shows that saving rate is a primary determinant of a country's steady state level of income. An increase in the saving rate raises investment causing the capital stock to grow toward a new steady state.



On the other hand, some economists say that high savings rate has contributed to Japan's slump during 1990s. High savings means lower consumption which according to IS-LM model translates into low aggregate demand and reduced income.

**Why Do Japanese consume so less or save so much?**

- It is harder for households to borrow in Japan
- In case of borrowing to purchase a house (the most common cause of borrowing), down payment rates are very high (up to 40%)
- Japanese Tax system encourages saving by taxing capital income very lightly
- Japanese are more risk averse and patient.

## CONSUMPTION THEORIES (CONTINUED)

### SUMMARIZATION:

#### JOHN MAYNARD KEYNES AND THE CONSUMPTION FUNCTION

The consumption function exhibits three properties that Keynes conjectured.

- The marginal propensity to consume  $c$  is between zero and one.
- The average propensity to consume falls as income rises.
- Consumption is determined by current income.

#### SIMON KUZNETS AND THE CONSUMPTION PUZZLE

- The failure of the secular-stagnation hypothesis and the findings of Kuznets both indicated that the average propensity to consume is fairly constant over time.
- This presented a puzzle: why did Keynes' conjectures hold up well in the studies of household data and in the studies of short time-series, but fail when long time series were examined?

#### IRVING FISHER AND INTERTEMPORAL CHOICE

The economist Irving Fisher developed the model with which economists analyze how rational, forward-looking consumers make intertemporal choices-- that is, choices involving different periods of time.

The model illuminates

- The constraints consumers face,
- The preferences they have, and
- How these constraints and preferences together determine their choices about consumption and saving.

When consumers are deciding how much to consume today versus how much to consume in the future, they face an intertemporal budget constraint, which measures the total resources available for consumption today and in the future.

#### FRANCO MODIGLIANI AND THE LIFE-CYCLE HYPOTHESIS

In the 1950's, Franco Modigliani, Ando and Brumberg used Fisher's model of consumer behavior to study the consumption function. One of their goals was to study the consumption puzzle. According to Fisher's model, consumption depends on a person's lifetime income. Modigliani emphasized that income varies systematically over people's lives and that saving allows consumers to move income from those times in life when income is high to those times when income is low. This interpretation of consumer behavior formed the basis of his life-cycle hypothesis.

#### THE HYPOTHESIS

Most people plan to stop working at about age 65, and they expect their incomes to fall when they retire, but don't want a drop in standard of living characterized by consumption. Suppose a consumer expects to live another  $T$  years, has wealth of  $W$  and expects to earn income  $Y$  until she retires  $R$  years from now.

What level of consumption will the consumer choose to have a smooth consumption over her life?

#### THE LIFE-CYCLE CONSUMPTION FUNCTION

The Lifetime resources of consumer for  $T$  years are wealth  $W$  and lifetime earnings of  $R \times Y$  (assuming interest rate to be zero). To have smoothest consumption over lifetime, she divides such that:

$$C = (W + RY) / T \quad \text{or}$$

$$C = (1 / T) W + (R / T) Y$$

If she expects  $T = 50$  and  $R = 30$ , then the consumption function will be

$$C = 1 / 50W + 30/50Y \text{ or}$$

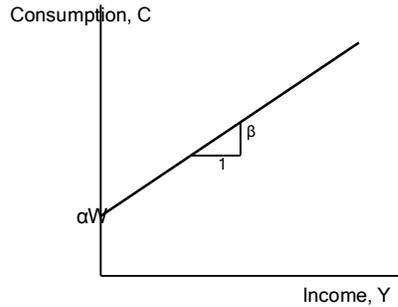
$$C = 0.02W + 0.6Y$$

Generalizing for Aggregate Consumption function of the economy:

$$C = \alpha W + \beta Y$$

Where,  $\alpha = \text{MPC out of Wealth}$

$\beta = \text{MPC out of Income}$

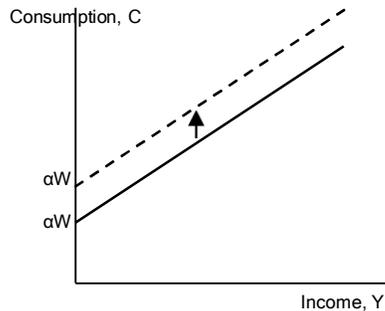


**SOLVING THE CONSUMPTION PUZZLE**

According to Life-cycle consumption function,

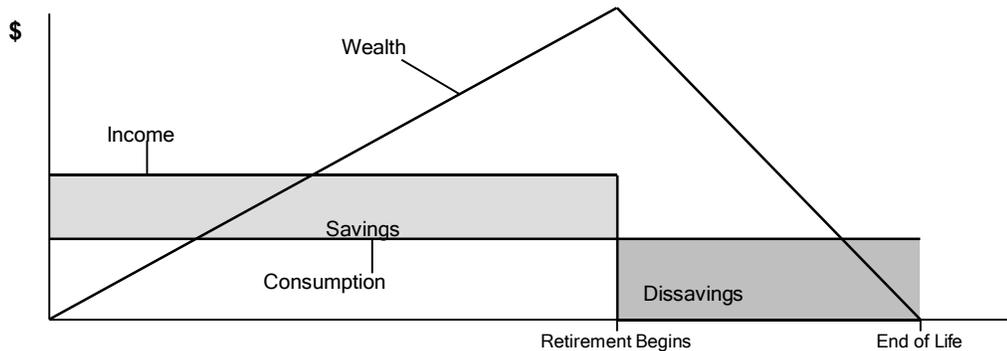
$$APC = C/Y = \alpha (W/Y) + \beta$$

Because, in short periods, wealth does not vary proportionately with incomes, High incomes correspond to Low APC. But over longer periods, wealth and incomes grow together, resulting in constant  $W/Y$  ratio and hence a constant APC



The upward shift prevents the APC from falling as income increases. Thus solving Keynes's puzzle.

**CONSUMPTION, INCOME AND WEALTH OVER LIFE-CYCLE**



## CONSUMPTION AND SAVING OF ELDERLY

Research findings show that elderly people do not dissave as much as the life cycle model predicts. In other words, the elderly do not run down their wealth as quickly as one would expect if they were trying to smooth their consumption over their remaining years of life.

### Reasons:

- They are concerned about unpredictable expenses. Additional saving that rises from uncertainty is called precautionary saving. This may be due to expecting a long life and to plan for a longer period of retirement.
- It is not completely persuasive considering the availability of annuity schemes of insurance companies and public health insurance plans.
- They may want to leave bequests to their children

## MILTON FRIEDMAN AND THE PERMANENT-INCOME HYPOTHESIS

In 1957, Milton Friedman proposed the permanent-income hypothesis to explain consumer behavior. Its essence is that current consumption is proportional to permanent income. Friedman's permanent-income hypothesis complements Modigliani's life-cycle hypothesis: both use Fisher's theory of the consumer to argue that consumption should not depend on current income alone.

But unlike the life-cycle hypothesis, which emphasizes that income follows a regular pattern over a person's lifetime, the permanent-income hypothesis emphasizes that people experience random and temporary changes in their incomes from year to year.

Friedman suggested that we view current income  $Y$  as the sum of two components, permanent income  $Y^P$  and transitory income  $Y^T$ .

$$Y = Y^P + Y^T$$

- Permanent Income is the part of income that people expect to persist in the future.
- Transitory income is the part of income that people do not expect to persist.

Friedman reasoned that consumption should depend primarily on permanent income because consumers use savings and borrowings to smooth consumption in response to transitory changes in income. Friedman approximation of consumption function is:

$$C = \alpha Y^P$$

While Average propensity to consume is:

$$APC = C/Y = \alpha Y^P / Y$$

- When  $Y > Y^P$ , APC Falls
- When  $Y < Y^P$ , APC rises

## ROBERT HALL AND THE RANDOM-WALK HYPOTHESIS

Robert Hall was first to derive the implications of rational expectations for consumption. He showed that if the permanent-income hypothesis is correct and if consumers have rational expectations, then changes in consumption over time should be unpredictable. When changes in a variable are unpredictable, the variable is said to follow a random walk.

According to Hall, the combination of the permanent-income hypothesis and rational expectations implies that consumption follows a random walk.

## INVESTMENT THEORIES

**Investment** is the most volatile component of GDP. When expenditure on goods and services fall during a recession, much of the decline is usually due to a drop in investment spending. Economists study investment to better understand the fluctuations in the economy's output of goods and services. The models of GDP, such as IS-LM model, were based on a simple investment function relating investment to real interest rate:  $I = I(r)$ . That function states that an increase in the real interest rate reduces Investment. Here we look more closely at the theory behind this investment function.

### THREE TYPES OF INVESTMENT SPENDING

We shall build models of each type of investment to explain the fluctuations in the economy. Also these models will shed light on the questions such as:

- Why investment is negatively related to the interest rate?
- What causes investment function to shift?
- Why does investment rise during booms and fall during recessions?

### BUSINESS FIXED INVESTMENT

The largest piece of investment spending (about  $\frac{3}{4}$  of total) is business fixed investment.

- Business: these investment goods are bought by firms for use in future production.
- Fixed: This spending is for capital that will stay put for a while (as opposed for inventory investment)

Business Fixed investment includes everything from fax machines to factories, computers to company cars. The standard model of business fixed investment is called the neoclassical model of investment. It examines the benefits and costs of owning capital goods. Here are three variables that shift investment:

- The marginal product of capital
- The interest rate
- Tax rules

To develop the model, imagine that there are two kinds of firms:

1. Production firms that produce goods and services using the capital that they rent
2. Rental firms that make all the investments in the economy.

In reality, however, most firms perform both functions

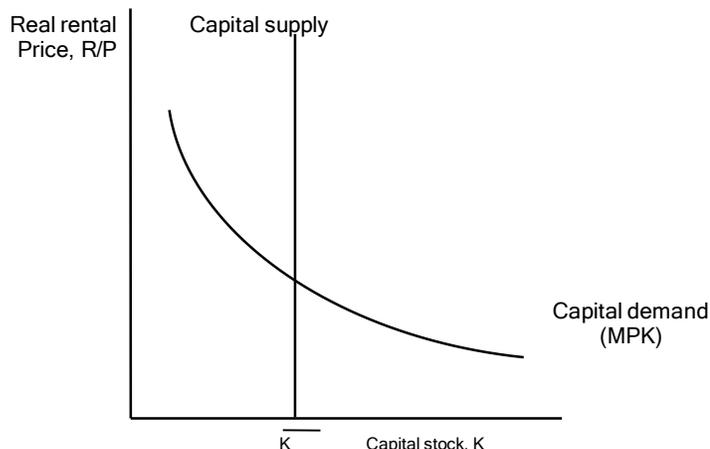
### THE RENTAL PRICE OF CAPITAL

A typical production firm decides how much capital to rent by comparing the cost and benefit of each unit of capital. The firm rents Capital at a rental rate  $R$  and sells its output at a price  $P$ . The real cost of a unit of capital to the production firm is  $R/P$ . The real benefit of a unit of capital is the marginal product of capital,  $MPK$  (the extra output produced with one more unit of capital).  $MPK$  falls as the amount of capital rises.

So, to maximize profit, the firm rents capital until the  $MPK$  falls to:

$$MPK = R/P$$

Hence  $MPK$  determines the downward sloping demand curve for capital for a firm. While at point in time, the amount of capital in an economy is fixed, so supply curve is fixed. The real rental price of capital adjusts to equilibrate the demand for capital and the fixed supply.



**The Cobb-Douglas production function** serves as a good approximation of how the actual economy turns capital and labor into goods and services. The Cobb-Douglas production function is:

$$Y = AK^\alpha L^{1-\alpha}$$

Where,

$Y \Rightarrow$  is output

$K \Rightarrow$  capital

$L \Rightarrow$  labor

$A \Rightarrow$  a parameter measuring the level of technology

$\alpha \Rightarrow$  a parameter between 0 and 1 that measures capital's share of output.

The marginal product of capital (MPK) for the Cobb-Douglas production function is:

$$MPK = \alpha A (L/K)^{1-\alpha}$$

Because the real rental price (R/P) equals MPK in equilibrium, we can write:

$$R/P = \alpha A (L/K)^{1-\alpha}$$

This expression identifies the variables that determine the real rental price.

It shows the following:

- The lower the stock of capital, the higher the real rental price of capital
- The greater the amount of labor employed, the higher the real rental price of capitals
- The better the technology, the higher the real rental price of capital.

Events that reduce the capital stock, or raise employment, or improve the technology, raise the equilibrium real rental price of capital.

### THE COST OF CAPITAL

The Rental firms, just like car rental firms merely buy capital goods and rent them out. Let's consider the benefit and cost of owning capital. The benefit of owning capital is the real rental price of capital R/P for each unit of capital it owns and rents out.

For each period of time that a firm rents out a unit of capital, the rental firm bears three costs:

1. Interest on their loans, which equals the purchase price of a unit of capital  $P_K$  times the interest rate,  $i$ , so  $iP_K$
2. The cost of the loss or gain on the price of capital denoted as  $-\Delta P_K$
3. Depreciation  $\delta$  defined as the fraction of value lost per period because of the wear and tear, so  $\delta P_K$

Therefore, Total cost of capital =  $iP_K - \Delta P_K + \delta P_K$

Or =  $P_K (i - \Delta P_K/P_K + \delta)$

The cost of capital depends upon the price of capital, the interest rate, rate of change of capital prices and the depreciation rate.

**Example:** A Car rental company buys cars for Rs.1, 000,000 each and rents them out to other businesses. If it faces an interest rate  $i$  of 10% p.a. so the interest cost,  $iP_k = \text{Rs.}100,000$  p.a.

Car prices are rising @ 6% per year, so excluding maintenance costs the firm gets a capital gain,  $\Delta P_k = \text{Rs.}60,000$  p.a

Cars depreciate @ 20% p.a. so loss due to wear and tear,

$$\delta P_k = \text{Rs.}200,000$$

$$\begin{aligned}\text{So, total cost of capital} &= iP_k - \Delta P_k + \delta P_k \\ &= 100,000 - 60,000 + 200,000 \\ &= \text{Rs.}240,000\end{aligned}$$

## INVESTMENT THEORIES (CONTINUED)

### THE COST OF CAPITAL

$$\begin{aligned}\text{Total cost of capital} &= iP_K - \Delta P_K + \delta P_K \\ &= P_K (i - \Delta P_K / P_K + \delta)\end{aligned}$$

The cost of capital depends upon the price of capital, the interest rate, rate of change of capital prices and the depreciation rate.

Assuming price of capital goods rises with the prices of other goods, so

$$\Delta P_K / P_K = \text{overall inflation rate, } \pi$$

Since,

$$r = i - \pi$$

$$\text{Cost of Capital} = P_K(r + \delta)$$

To express the cost of capital relative to other goods in the economy.

The real cost of capital-- the cost of buying and renting out a unit of capital measured in terms of the economy's output is:

$$\text{Real Cost of Capital} = (P_K / P) (r + \delta)$$

Where

$r \Rightarrow$  the real interest rate

$P_K / P \Rightarrow$  the relative price of capital.

### THE DETERMINANTS OF INVESTMENT

Now consider a rental firm's decision about whether to increase or decrease its capital stock.

For each unit of capital, the firm earns real revenue  $R/P$  and bears the real cost  $(P_K / P) (r + \delta)$ .

The real profit per unit of capital is

$$\begin{aligned}\text{Profit rate} &= \text{Revenue} - \text{Cost} \\ &= R/P - (P_K / P) (r + \delta).\end{aligned}$$

Because real rental price equals the marginal product of capital, we can write the profit rate as

$$\text{Profit rate} = \text{MPK} - (P_K / P) (r + \delta)$$

The change in the capital stock, called net investment depends on the difference between the MPK and the cost of capital.

- If the MPK exceeds the cost of capital, firms will add to their capital stock.
- If the MPK falls short of the cost of capital, they let their capital stock shrink.

Thus:

$$\Delta K = I_n [\text{MPK} - (P_K / P) (r + \delta)]$$

Where  $I_n ( )$  is the function showing how much net investment responds to the incentive to invest.

### THE INVESTMENT FUNCTION

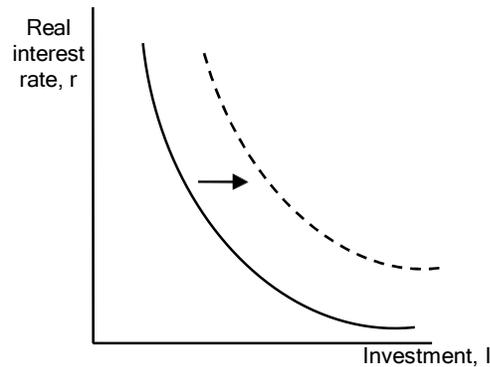
We can now derive the investment function in the neoclassical model of investment. Total spending on business fixed investment is the sum of net investment and the replacement of depreciated capital.

The investment function is:

$$I = I_n [\text{MPK} - (P_K / P) (r + \delta)] + \delta K$$

This model shows why investment depends on the real interest rate.

A decrease in the real interest rate lowers the cost of capital. It therefore raises the amount of profit from owning the capital and increases the incentive to accumulate more capital. Similarly an increase in real interest rate raises cost of capital and leads the firms to reduce their investment.



As  $r \downarrow$ , hence the downward slope of the investment function. Also, an outward shift in the investment function may be a result of an increase in the marginal product of capital. e.g. a technological innovation

Finally, we consider what happens as this adjustment of the capital stock continues over time.

- If the marginal product begins above the cost of capital, the capital stock will rise and the marginal product will fall.
- If the marginal product of capital begins below the cost of capital, the capital stock will fall and the marginal product will rise.
- Eventually, as the capital stock adjusts, the MPK approaches the cost of capital.

When the capital stock reaches a steady state level, we can write:

$$MPK = (PK/P)(r + \delta)$$

Thus, in the long run, the MPK equals the real cost of capital. The speed of adjustment toward the steady state depends on how quickly firms adjust their capital stock, which in turn depends on how costly it is to build, deliver and install new capital.

## TAXES AND INVESTMENT

Tax laws influence the firms' incentives to accumulate the capital in many ways. Sometimes policymakers change the tax laws in order to shift the investment function and influence aggregate demand. Here we discuss two of the most important provisions of corporate taxes:

- Corporate Income Tax
- Investment Tax Credit

**Corporate income tax** is a tax on corporate profits, and its effect on investment depends on how the law defines profit for the purpose of taxation.

Suppose, at first, the law says:

$$\text{Profit rate} = R/P - (PK/P)(r + \delta)$$

In this case, even though firms would be sharing a fraction of their income with the government, it would still be rational for them to invest if

$$R/P > (PK/P)(r + \delta)$$

But in reality the definition of law is quite different than this.

- Treatment of depreciation
- Theoretically: current value of depreciation
- Tax laws: depreciation at historical cost

**The Investment Tax Credit** is a tax provision that encourages the accumulation of capital. It reduces a firm's taxes by a certain amount for each unit of money spent on capital goods. Since the firm recoups part of its expenditures on new capital in lower taxes, the credit reduces the effective purchase price of a unit of capital  $P_k$ . Thus reducing the cost of capital and raising investment.

## SWEDISH INVESTMENT FUNDS SYSTEM

Tax incentives for investment are one tool policy makers can use to control aggregate demand.

For example, an increase in the investment tax credit reduces the cost of capital, shifts investment function upward, and raises the aggregate demand. From mid-50s to mid-70s the govt. of Sweden attempted to control aggregate demand by encouraging or discouraging investment, through a system called Investment Fund subsidized investment. In case of economic slowdown, the authorities offered a temporary investment subsidy, and in case of economic recovery, revoked it. Eventually subsidy became a permanent feature of Swedish tax policy.

## INVESTMENT THEORIES (CONTINUED)

### THE STOCK MARKET AND TOBIN'S $q$

The term stock refers to the shares in the ownership of corporations. Stock market is the market in which these shares are traded. The Nobel-Prize-winning economist James Tobin proposed that firms base their investment decisions on the following ratio, which is now called *Tobin's  $q$* :

$$q = \frac{\text{Market Value of Installed Capital}}{\text{Replacement Cost of Installed Capital}}$$

The numerator of Tobin's  $q$  is the value of the economy's capital as determined by the stock market. The denominator is the price of capital as if it were purchased today.

Tobin conveyed that net investment should depend on whether  $q$  is greater or less than 1.

- If  $q > 1$ , then firms can raise the value of their stock by increasing capital,
- if  $q < 1$ , the stock market values capital at less than its replacement cost and thus, firms will not replace their capital stock as it wears out.

Tobin's  $q$  and neo-classical model are closely related, since Tobin's  $q$  measures the expected future profitability as well as the current profitability.

If the MPK exceeds cost of capital, the firms are earning profits on their installed capital, making rental firms desirable to own, raising market value of stocks of such firms, implying a high value of  $q$

### THE STOCK MARKET AS AN ECONOMIC INDICATOR

Although the volatility of stock market can give false signals about the future of economy, yet one should not ignore the link between the two. Changes in stock market often reflect changes in GDP. Whenever stock market experiences a substantial decline, we should be ready for an upcoming recession.

**Why do stock prices and economic activity tend to fluctuate together?**

#### Tobin's $q$ and AD-AS Model

Suppose there occurs a fall in stock prices. Since replacement cost of capital is stable, this will result in a fall in Tobin's  $q$ , reflecting investors' pessimism about the current or future profitability of capital.

#### Some Additional Reasons

- A fall in stock prices makes people poorer, depressing their spending, resulting in reduced aggregate demand
- Fall in stock prices reflect bad news about technological progress and economic growth, resulting in slow expansion of natural rate of output.

### FINANCING CONSTRAINTS

When a firm wants to invest in new capital, e.g. by building a new factory, it raises the funds in financial markets by

- Obtaining loans from banks
- Selling bonds to public
- Selling shares in future profits on stock market

Neo classical model assumes that if a firm is willing to pay cost of capital, financial markets will make the funds available. But sometimes firms face Financing constraints, limiting the amount of funds they can raise from financial market. So the amount a firm can spend on new capital goods is limited to the amount it is currently earning.

**For example**, a recession reduces employment, rental price of capital and profits. If the firm expects the recession to be short lived, it will continue investing for long term profitability, thus having a small effect on Tobin's  $q$ .

So the firm that can raise funds in financial markets will face a small effect of recession on the investment. While in case of firms facing constraints, the fall in current profits restrict the spending on new capital goods and may prevent such firms from making profitable investment.

## RESIDENTIAL INVESTMENT

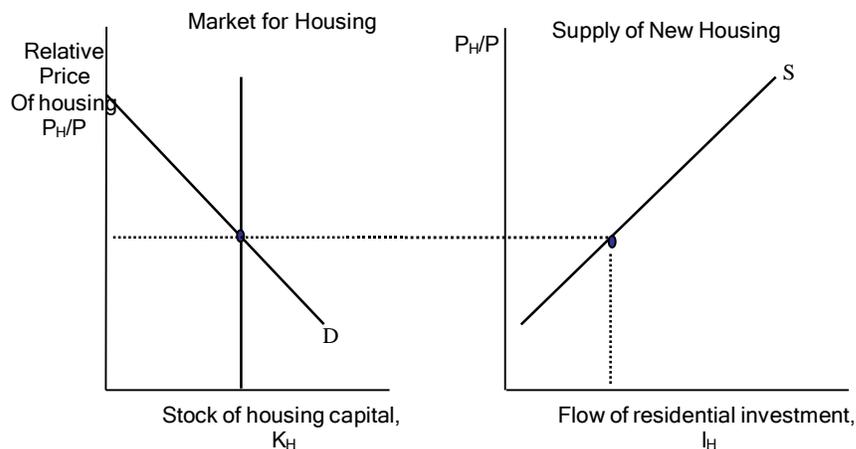
We will now consider the determinants of residential investment by looking at a simple model of the housing market. Residential investment includes the purchase of new housing both by people who plan to live in it themselves and by landlords who plan to rent it to others.

To keep things simple, we shall assume that all housing is owner-occupied.

There are two parts to the model:

- 1) The market for the existing stock of houses determines the equilibrium housing price
- 2) The housing price determines the flow of residential investment.

The relative price of housing adjusts to equilibrate supply and demand for the existing stock of housing capital. Construction firms buy materials and hire labor to build the houses and then sell them at market price. Their costs depend on the overall price level  $P$  while their revenue depends on the price of houses  $P_H$ . The Higher the  $P_H$ , the greater incentive to build house.



This model of residential investment is much similar to  $q$  theory of business fixed investment, which states that business fixed investment depends on the market price of installed capital relative to its replacement cost, which in turn depends on expected profits from owning installed capital. The residential investment depends on the relative price of housing, which in turn depends on demand for housing, depending on the imputed rent that individuals expect to receive from their housing.

**INVESTMENT THEORIES (****INVENTORY INVESTMENT**

Inventory investment, the goods that businesses put up for sale, is negligible and of great significance. It is one of the most volatile components of GDP. Its volatility makes it critical in the study of economic fluctuations. Firms replenish their inventory as goods are sold, and invest in new inventory.

1. When sales are high, the firm produces less inventory. This is called **production smoothing**.
2. Holding inventory may allow firms to operate more efficiently. Thus, we can view **inventories as a factor of production**.
3. Also, firms don't want to run out of goods when sales are unexpectedly high. This is called **stock-out avoidance**.
4. Lastly, if a product is only partially completed, the components are still counted in inventory, and are called, **work in process**.

**SEASONAL FLUCTUATION AND PRODUCTION SMOOTHING**

Contrary to the expectations of many economists and researchers, firms do not use inventories to smooth production over time. The clearest evidence comes from industries with seasonal fluctuations in demand. e.g. fan manufacturing. One would expect that firms would build up inventories in times of low sales and draw them down in times of high sales. Yet in most industries firms do not use inventories to smooth production over the year, rather seasonal pattern matches seasonal pattern in sales.

**THE ACCELERATOR MODEL OF INVENTORIES**

The **accelerator model** assumes that firms hold a stock of inventories that is proportional to the firm's level of output. When output is high, manufacturing firms need more materials and supplies on hand, and more goods in process of completion. When Economy is booming, retail firms want to have more merchandise on their shelves to show customers.

Thus, if  $N$  is the economy's stock of inventories and  $Y$  is output, then

$$N = \beta Y$$

Where  $\beta$  is a parameter reflecting how much inventory firms wish to hold as a proportion of output. Inventory investment  $I$  is the change in the stock of inventories  $\beta \Delta Y$ .

Therefore,

$$I = \Delta N = \beta \Delta Y$$

The accelerator model predicts that inventory investment is proportional to the change in output

- When output rises, firms want to hold a larger stock of inventory, so inventory investment is high
- When output falls, firms want to hold a smaller stock of inventory, so they allow their inventory to run down, and inventory investment is negative.

The model says that inventory investment depends on whether the economy is speeding up or slowing down.

**INVENTORIES AND THE REAL INTEREST RATE**

Like other components of investment, inventory investment depends on the real interest rate. When a firm holds a good in inventory and sells it tomorrow rather than selling it today, it gives up the interest it could have earned between today and tomorrow. Thus, the real interest rate measures the opportunity cost of holding inventories. When the interest rate rises, holding inventories becomes more costly, so rational firms try to reduce their stock. Therefore, an increase in the real interest rate depresses inventory investment.

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 \*\*Inventory Investment and Its Dynamics:\*\*

- **\*\*Significance of Inventory Investment:\*\*** Small in spending but vital for studying economic fluctuations.
- **\*\*Negative Inventory Investment:\*\*** In recessions, inventory declines as goods are sold.
- **\*\*Production Smoothing:\*\*** High sales lead to lower production to match inventory removal.

## MONEY & BANKING

### MONEY SUPPLY

Earlier, we introduced the concept of money supply in a highly simplified way. We defined quantity of money as the number of rupees held by public, and assumed that central bank controls the supply of money by increasing or decreasing the number of rupees in circulation through open-market operations. Although a good approximation, this definition omits the role of banking system in determining the money supply.

Here, we'll see that the money supply is determined not only by the Central Bank, but also by the behavior of households (which hold money) and banks (where money is held).

Recall, the **Money supply includes both currency in the hand of public and deposits at banks that households use on demand for transactions.**

$$M = C + D$$

Where

M ---> Money Supply

C ---> Currency

D ---> Demand Deposits

### 100% RESERVE BANKING

Imagine a world without banks, where all the money takes the form of currency, and the quantity of money is simply the amount of currency that public holds (assume \$1,000). Now a new bank comes in and accepts deposits but does not make loans. Its only purpose is to provide a safe place for depositors to keep money.

- The deposits that banks have received but have not lent out are called reserves.
- Some Reserves are held in the vaults of local banks but most are held at the central bank.

Consider the case where all deposits are held as reserves: banks accept deposits, place the money in reserve, and leave the money there until the depositor makes a withdrawal or writes a check against the balance. In a 100% reserve banking system, all deposits are held in reserve and thus the banking system does not affect the supply of money.

Suppose that households deposit the economy's entire \$1,000 in First bank. This bank's balance sheet will look like:

Assets		Liabilities	
Reserves	\$1,000	Deposits	\$1,000

The bank is not making loans so it is not earning profit rather a small fee to cover its cost. The money supply in the economy before and after the creation of bank remains the same, i.e. \$1,000. So 100% reserve deposit does not affect money supply in economy

### FRACTIONAL RESERVE BANKING

Now, if the banks start to use some of their deposits to make loans (e.g. to households for house finance and to firms for capital finance), they can charge interest on the loans. The banks must keep some reserve on hand so that reserves are available whenever depositors want to make withdrawals. As long as the amount of new deposits approximately equals the amount of withdrawals, a bank need not keep all its deposits in reserves.

- **Note:** a *reserve-deposit ratio* is the fraction of deposits kept in reserve. **Excess reserves** are reserves above the reserve requirement.
- **Fractional-reserve banking**, a system under which banks keep only a fraction of their deposits in reserve. In a system of fractional reserve banking, banks create money.

## MONEY & BANKING (CONTINUED)

### HOW DOES THE CENTRAL BANK CONTROL THE MONEY SUPPLY?

- Open Market Operations
- Changing the Reserve Requirements
- Changing Discount rate

### THREE INSTRUMENTS OF MONEY SUPPLY

- **Open market operations** are the purchase and sale of government bonds by the central bank. When the central bank buys bonds from public, the money it pays for the bonds increases the monetary base and thus increases the money supply. When the central bank sells the bonds to the public, the money it receives reduces monetary base and hence reduce money supply
- **Reserve requirements** are central banks regulations that impose on banks a minimum reserve-deposit ratio. An increase in reserve requirements raises reserve deposit ratio and thus lowers the money multiplier and the money supply
- **The Discount rate** is the interest rates that central bank charges when it lends to the banks. Banks borrow from central bank when they find themselves with too few reserves to meet reserve requirements. The lower the discount rate, the cheaper are borrowed reserves and more demands for such loans. Hence a reduction in discount rate raises the monetary base and the money supply.

Although these instruments give central bank substantial power to influence the money supply, yet it can't do it perfectly. Bank discretion in conditioning business can cause the money supply to change the way central bank did not anticipate.

- Excessive Reserves
- No limit on the amount of bank borrowings from discount window

### MONEY DEMAND

#### CLASSICAL THEORY OF MONEY DEMAND

The Quantity Theory of Money assumes that the demand for real money balances is directly proportional to income,

$$(M/P)_d = kY$$

Where k is a constant measuring how much people want to hold for every dollar of income.

#### KEYNESIAN THEORY OF MONEY DEMAND

It presents a more realistic money demand function where the demand for real money balances depends on i and Y:

$$(M/P)_d = L(i, Y)$$

Recall, that money serves three functions

- Unit of Account
- A store of value
- A medium of Exchange

The first function can not by itself generate any demand for money, because we can quote prices in any currency without holding any amount of it. So we shall focus on the rest of the two functions as we look at theories of money demand

#### PORTFOLIO THEORIES OF MONEY DEMAND

Theories of money demand that emphasize the role of money as a store of value are called portfolio theories. According to these theories, people hold money as part of their portfolio of assets.

The key point is that money offers a different combination of risk and return than other assets, particularly a safe return (nominal). While other assets may fall in both real and nominal terms. These theories predict that demand for money should depend on the risk and return offered by money and other assets.

Also money demand should depend on total wealth, because wealth measures the size of portfolio to be allocated among money and other assets.

So we may write the money demand function as

$$(M/P)^d = L(r_s, r_b, \pi^e, W)$$

Where

$r_s$  = expected real return on stock

$r_b$  = expected real return on bonds

$\pi^e$  = expected inflation rate

$W$  = real wealth

- If  $r_s$  or  $r_b$  rises, money demand reduces, because other assets become more attractive.
- A rise in  $\pi^e$  also reduces the money demand because money becomes less attractive.
- An increase in  $W$  raises money demand because higher wealth means higher portfolio.

**Money Demand Function L(i, Y): A useful simplification:**

- Uses real income Y as proxy for real wealth W
- Nominal interest rate  $i = r_b + \pi^e$

**Are these theories useful for studying money demand?**

The answer depends on which measure of money are we using.

SYMBOL	ASSETS INCLUDED	
C	Currency	
M1	C + demand deposits,	M1: This includes currency (C) plus the money that you can easily access and use for everyday transactions. It's like the money you can spend quickly. It includes demand deposits (checking accounts), travelers' checks, and other checkable deposits.
M2	M1 + small time deposits	
M3	M2 + large time deposits Mutual fund balances	

Economists say that M1 is a dominated assets and stress that people hold money, unlike other assets, to make purchases. Thus it is not optimal for people to hold money as part of their portfolio and portfolio theories cannot explain the demand for these dominated forms of money. But these theories would be more plausible if we adopt a broader measure of money like M2.

**TRANSACTIONS THEORIES OF MONEY DEMAND**

Theories which emphasize the role money as a medium of exchange acknowledge that money is a dominated assets and stress that people hold money, unlike other assets, to make purchases. These theories best explain why people hold narrow measure of money as opposed to holding assets that dominate them. These theories take many forms depending on how one models the process of obtaining money and making transactions assuming:

- Money has the cost of earning a low rate of return
- Money makes transactions more convenient

**BAUMOL-TOBIN MODEL OF CASH MANAGEMENT**

One prominent model to explain the money demand function is Baumol-Tobin Model developed in 1950. This model analyzes the cost and benefits of holding money.

- Benefit: Convenience (much less trips to banks)
- Costs: foregone interest on money had it been deposited in a savings account

**Example:**

A person plans to spend Y dollars over the course of an year (assuming constant price levels and real spending). What should be the optimal size of cash balances for him?

**Possibilities**

- Withdraw Y dollars at the beginning of the year and gradually spend the money balance averaging Y/2 over the year
- Draw Y/2 at the beginning of year, spend it in six months then draw the rest Y/2 to be spent in next 1/2 year. Average balance = Y/4

**Generalizing:** money holding vary between Y/N and zero, averaging Y/(2N), where N is the number of trips to bank

**One implication of the Baumol-Tobin model** is that any change in the fixed cost of going to the bank F alters the money demand function-- that is, it changes the quantity of money demanded for a given interest rate and income.

**MONEY CREATION**

Assume each bank maintains a *reserve-deposit ratio (rr)* of 20% and that the initial deposit is \$1000.

First bank Balance Sheet	
Assets	Liabilities
Reserve \$200	Deposits \$1,000
Loans \$800	

Second bank Balance Sheet	
Assets	Liabilities
Reserve \$160	Deposits \$800
Loans \$640	

Third bank Balance Sheet	
Assets	Liabilities
Reserve \$128	Deposits \$640
Loans \$512	

Mathematically, the amount of money the original \$1000 deposit creates is:

Original Deposit	= \$1000
First bank Lending	= (1-rr) × \$1000
Second bank Lending	= (1-rr) <sup>2</sup> × \$1000
Third bank Lending	= (1-rr) <sup>3</sup> × \$1000
Fourth bank Lending	= (1-rr) <sup>4</sup> × \$1000
	⋮
	⋮

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Total Money Supply	= [1 + (1-rr) + (1-rr) <sup>2</sup> + (1-rr) <sup>3</sup> + ...] × \$1000
	= (1/rr) × \$1000
	= (1/.2) × \$1000
	= \$5000

The banking system’s ability to create money is the primary difference between banks and other financial institutions.

**Financial intermediation:**

Financial markets have the important function of transferring the economy’s resources from households (who wish to save some of their income for the future) to those households and firms that wish to borrow to buy investment goods to be used in future production. The process of transferring funds from savers to borrowers is called financial intermediation.

**A MODEL OF MONEY SUPPLY**

**Three exogenous variables:**

- The **monetary base B** is the total number of dollars held by the public as currency C and by the banks as reserves R.
- The **reserve-deposit ratio rr** is the fraction of deposits D that banks hold in reserve R.
- The **currency-deposit ratio cr** is the amount of currency C people hold as a fraction of their holdings of demand deposits D.

**Definitions of money supply and monetary base:**

$$M = C + D$$

$$B = C + R$$

Solving for M as a function of 3 exogenous variables:

$$M/B = \frac{C/D + 1}{C/D + R/D}$$

Making substitutions for the fractions above, we obtain:

$$M = \frac{cr + 1}{cr + rr} \times B$$

Lets call this money multiplier, m

So

$$M = m \times B$$

Because the monetary base has a multiplied effect on the money supply, the monetary base is sometimes called *high-powered money*.

**An Example**

Suppose, monetary base B is \$500 billion, the reserve deposit ratio rr is 0.1 and currency deposit ratio cr is 0.6

**The money multiplier is:**

$$m = \frac{0.6 + 1}{0.6 + 0.1} = 2.3$$

And the money supply is:

$$M = 2.3 \times \$ 500 \text{ billion} = \$1,150 \text{ billion}$$

Let's go back to our three exogenous variables to see how their changes cause the money supply to change:

1. The money supply M is proportional to the monetary base B. So, an increase in the monetary base increases the money supply by the same percentage.
2. The lower the reserve-deposit ratio rr (R/D), the more loans banks make, and the more money banks create from every dollar of reserves.
3. The lower the currency-deposit ratio cr (C/D), the fewer dollars of the monetary base the public holds as currency, the more base dollars banks hold in reserves, and the more money banks can create. Thus a decrease in the currency-deposit ratio raises the money multiplier and the money supply.